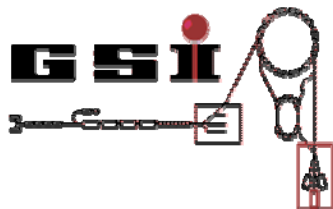
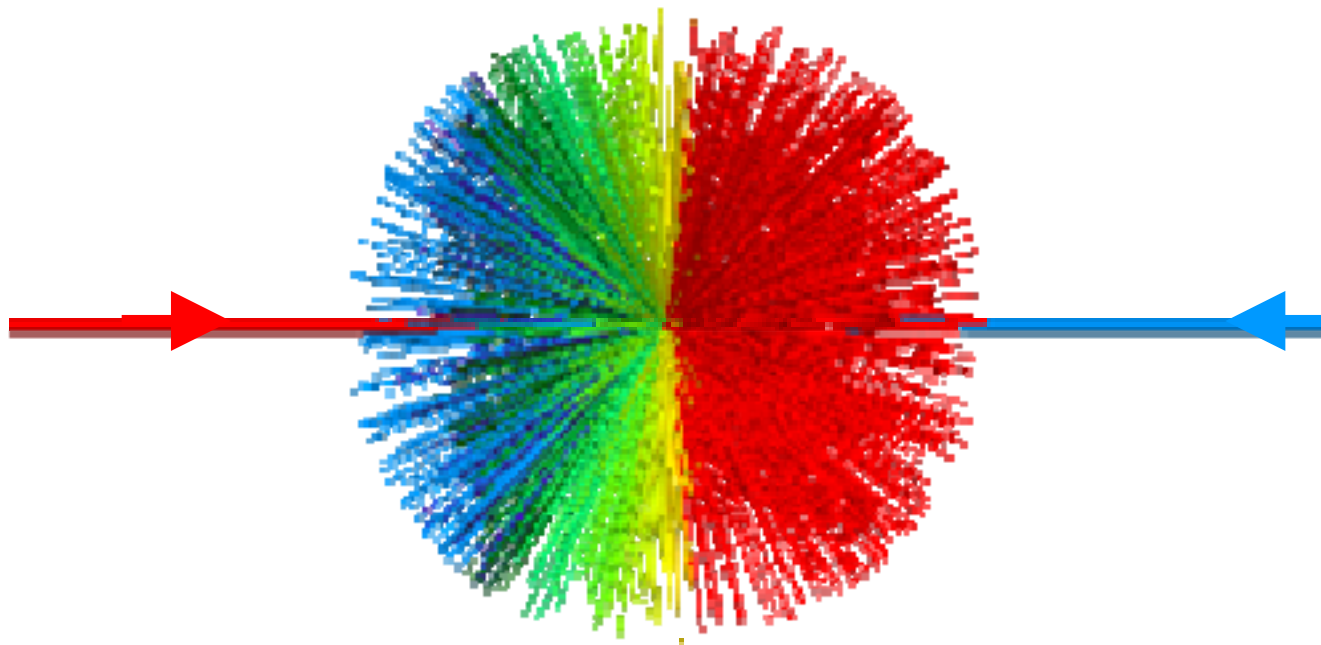


Towards a test of time dilation:



*Spectroscopy of lithium ions at
34% of the speed of light with
sub-Doppler linewidth*





Introduction: test theories for SRT

Tools for modern test of time dilation

Status of the experiment at GSI and first signals

Results & Outlook

Why testing time dilation?



Lorentz invariance is a fundamental constituent

in the *standard model* of particle physics as well as
in the *theory of general relativity*

Special Relativity ↔ Lorentz transformations

Standard Model



electro-magnetic
force



nuclear weak
force



nuclear strong
force



General Relativity



gravitational force

In some models hypothetical Lorentz violations are included

Lorentz violation could be a **revealed by experiment** as a *signature of new physics*

Hypothetical deviations can be included as quantitative parameters in test theories

Dynamical / kinematical test theory



Any test theory gives: a base to **compare different experiments** and **parameterize possible violations**

Kinematical test theory

(e.g. Robertson, **Mansouri & Sexl**)

generalized Lorentz transformation

preferred frame assumed

only a few parameters are needed

Dynamical test theory

(e.g. Standard Model Extension)

(Kostelecký et al.)

small extension of the SM Lagrangian

can describe particle couplings

several hundreds of parameters

deformed "lightcone"



- *no longer* Lorentzian
spacetime structure

- vacuum remains
empty

lightcone



- structure of underlying
spacetime *unchanged*

- vacuum contains *back-*
ground with vectors
and pseudo vectors

Dynamical / kinematical test theory



Any test theory gives: a base to **compare different experiments** and **parameterize possible violations**

Kinematical test theory

(e.g. Robertson, **Mansouri & Sexl**)

generalized Lorentz transformation

preferred frame assumed
only a few parameters

Dynamical test theory

(e.g. Standard Model)

modification of the SM Lagrangian

can describe particle couplings
several hundreds of parameters

BUT!

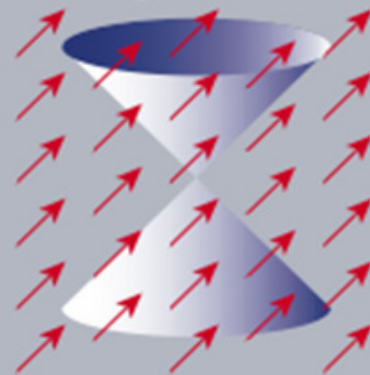
No minimum limit for Lorentz violation is stated by (test) theories!

deformed "lightcone"



- *no longer* Lorentzian spacetime structure
- vacuum remains *empty*

lightcone



- structure of underlying spacetime *unchanged*
- vacuum contains *background with vectors and pseudo vectors*

Mansouri-Sexl (MS) test theory

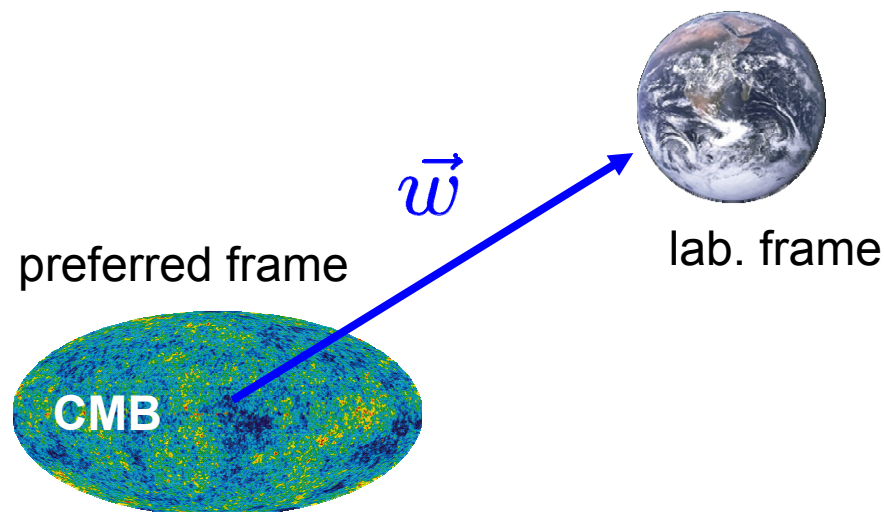


Generalized Lorentz transformations

$$\begin{aligned}
 T &= \frac{1}{a} \left(t + \frac{wx}{c_0} \right) \\
 X &= \frac{x}{b} + \frac{wc_0}{a} \left(t + \frac{wx}{c_0} \right) \\
 Y &= \frac{y}{d}, \quad Z = \frac{z}{d}
 \end{aligned}$$

for special relativity

$$\begin{aligned}
 a &= b^{-1} = \underbrace{\sqrt{1 - w^2}}_{\gamma^{-1}} \\
 d &= 1
 \end{aligned}$$



Assumptions:

- preferred “ether” frame Σ (CMB ?)
- only in Σ the light speed is isotropic
- lab. frame is moving with along the x-axis

expansion in velocity terms

$$\begin{aligned}
 a(w^2) &= (1 - w^2)^{1/2} (1 + \delta\alpha \cdot w^2 + \dots) \\
 b(w^2) &= (1 - w^2)^{-1/2} (1 + \delta\beta \cdot w^2 + \dots) \\
 d(w^2) &= (1 + \delta \cdot w^2 + \dots)
 \end{aligned}
 \quad \left. \begin{array}{l} \longrightarrow \\ \} \end{array} \right\} \begin{array}{l} \text{time dilation} \\ \text{(Ives-Stilwell)} \\ \text{isotropy of space} \\ \text{(Michelson-Morley \& Kennedy-Thorndike)} \end{array}$$

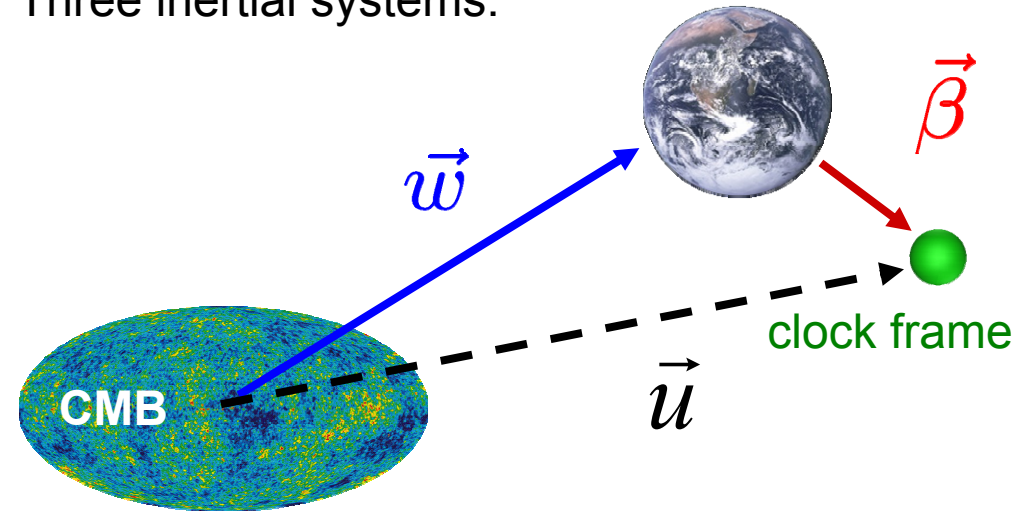
Time dilation in the MS-framework



Generalized Lorentz transformations

$$\begin{aligned}
 T &= \frac{1}{a} \left(t + \frac{wx}{c_0} \right) \\
 X &= \frac{x}{b} + \frac{wc_0}{a} \left(t + \frac{wx}{c_0} \right) \\
 Y &= \frac{y}{d}, \quad Z = \frac{z}{d}
 \end{aligned}$$

Three inertial systems:



lead to a modified Lorentz factor:

$$\gamma_{MS} = \gamma \cdot \left[1 + \delta\alpha \cdot (\beta^2 + 2 \cdot \vec{\beta} \cdot \vec{w}) + \dots \right]$$

Test parameter

is a function of

$$\vec{w} = 350 \text{ km/s}$$

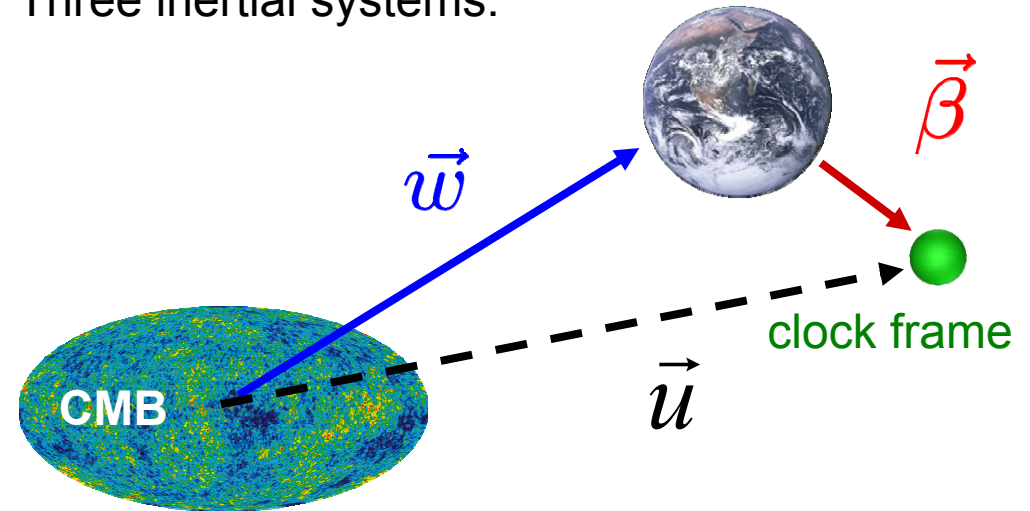
Time dilation in the MS-framework



Generalized Lorentz transformations

$$\begin{aligned}
 T &= \frac{1}{a} \left(t + \frac{wx}{c_0} \right) \\
 X &= \frac{x}{b} + \frac{wc_0}{a} \left(t + \frac{wx}{c_0} \right) \\
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 \end{aligned}$$

Three inertial systems:



lead to a modified Lorentz factor:

$$\gamma_{MS} = \gamma \cdot \left[1 + \delta\alpha \cdot \left(\beta^2 + 2 \cdot \vec{\beta} \cdot \vec{w} \right) + \dots \right]$$

Test parameter $\delta\alpha$ is a function of β^2

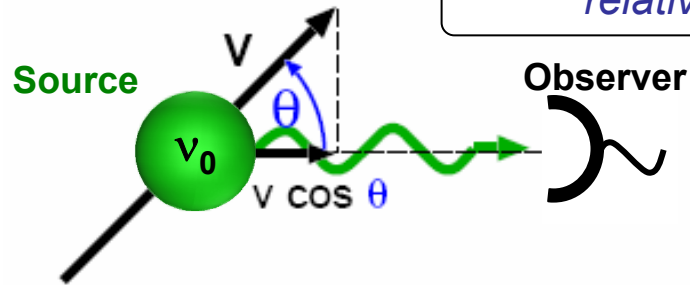
we neglect sidereal term $2 \cdot \vec{\beta} \cdot \vec{w}$

$\vec{w} = 350 \text{ km/s} \ll \vec{\beta} \sim 10\,000 \text{ km/s}$

Test of time dilation



relativistic Doppler effect



$$v = v_0 \frac{1}{\gamma (1 - \beta \cos \theta)}$$

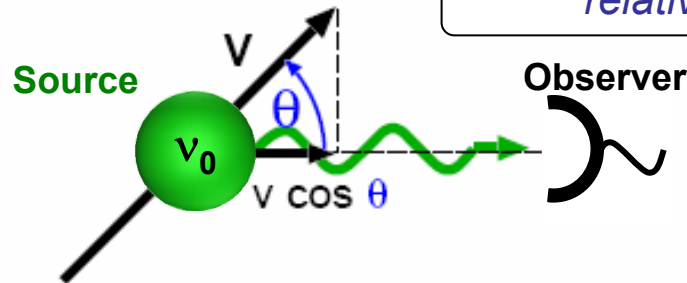
$$\beta = \frac{v}{c}$$

$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

Test of time dilation



relativistic Doppler effect



$$\nu = \nu_0 \frac{1}{\gamma (1 - \beta \cos \theta)}$$

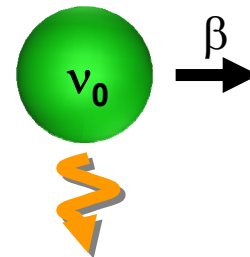
$$\beta = \frac{v}{c}$$

$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

Einstein proposed 1907:

$$\theta = 90^\circ$$

$$\frac{\nu_0}{\nu} = \gamma$$

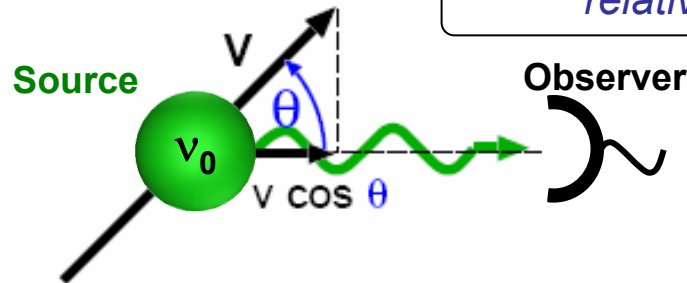


→ Experimentally impossible to measure light emitted only at 90°

Test of time dilation



relativistic Doppler effect



$$v = v_0 \frac{1}{\gamma (1 - \beta \cos \theta)}$$

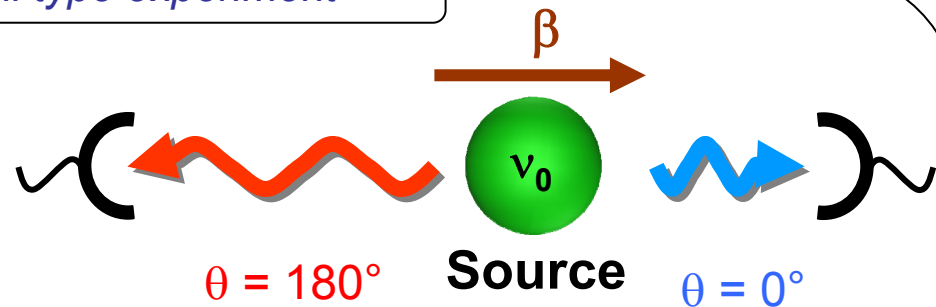
$$\beta = v/c$$

$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

Ives-Stilwell type experiment

$$v_p = \frac{v_0}{\gamma \cdot (1 - \beta)}$$

$$v_a = \frac{v_0}{\gamma \cdot (1 + \beta)}$$

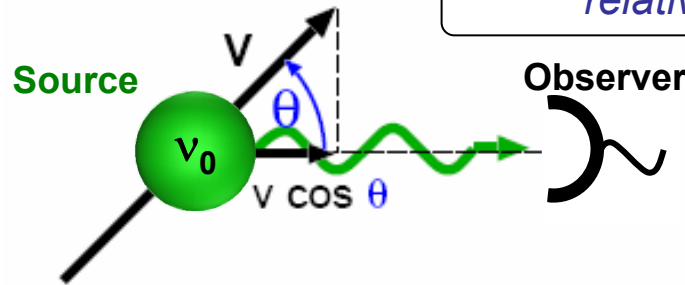


$$\frac{v_a \cdot v_p}{v_0^2} = \gamma^2 \cdot (1 - \beta^2) \equiv 1$$

Test of time dilation



relativistic Doppler effect



$$\nu = \nu_0 \frac{1}{\gamma (1 - \beta \cos \theta)}$$

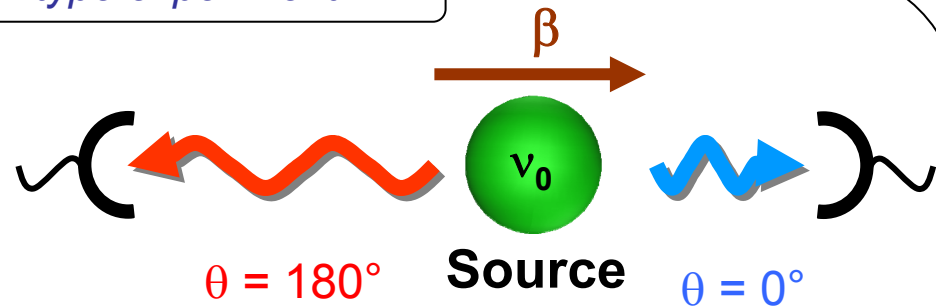
$$\beta = \frac{v}{c}$$

$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

Ives-Stilwell type experiment

$$\nu_p = \frac{\nu_0}{\gamma \cdot (1 - \beta)}$$

$$\nu_a = \frac{\nu_0}{\gamma \cdot (1 + \beta)}$$



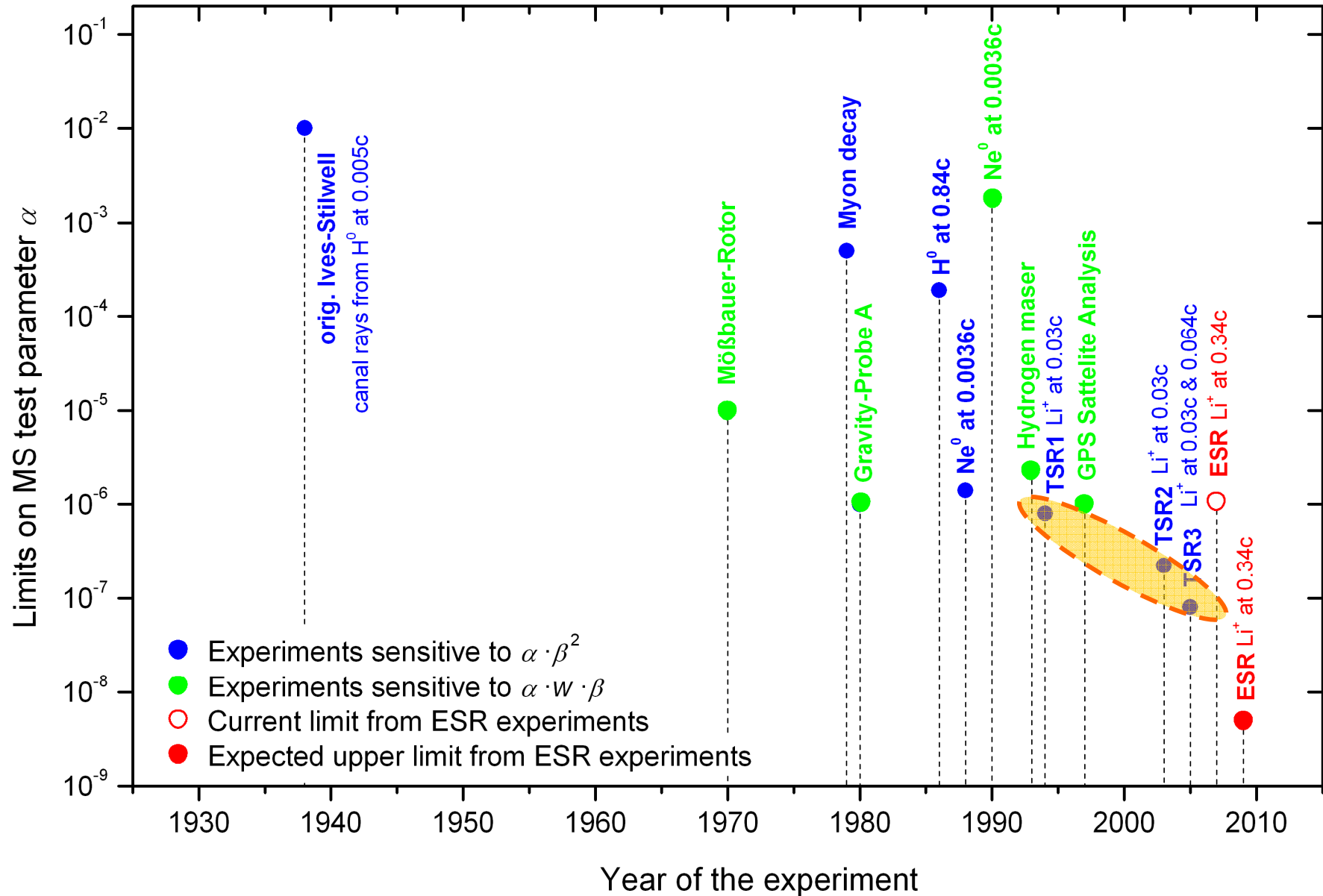
$$\frac{\nu_a \cdot \nu_p}{\nu_0^2} = \gamma^2 \cdot (1 - \beta^2) \stackrel{?}{=} 1 + \epsilon$$

$$\gamma \xrightarrow{\epsilon \neq 0} \gamma_{MS}$$

$$= \gamma_{MS}^2 \cdot (1 - \beta^2) = 1 + 2 \cdot \delta\alpha \cdot \beta^2 + (\delta\alpha + 2 \cdot \delta\alpha_2) \cdot \beta^4 + \dots$$

Time Dilation can be tested via comparing three optical frequencies

Evolution of time dilation tests



Modern Ives-Stilwell experiment

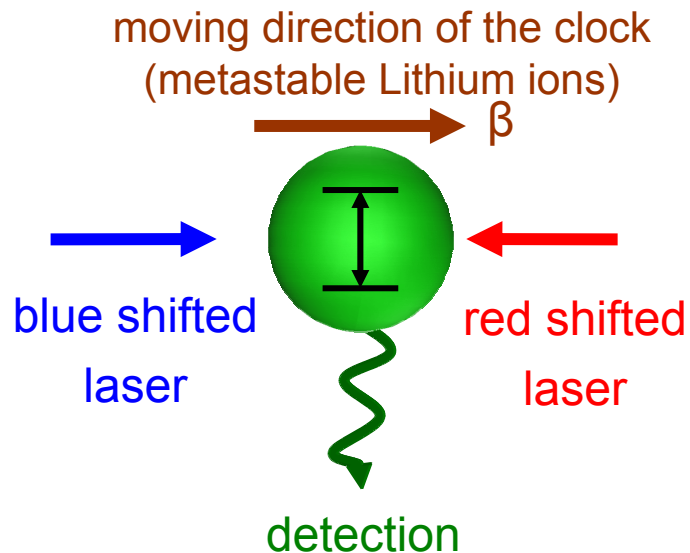


$$\frac{v_a \cdot v_p}{v_0^2} = 1 + 2 \cdot \delta\alpha \cdot \beta^2$$

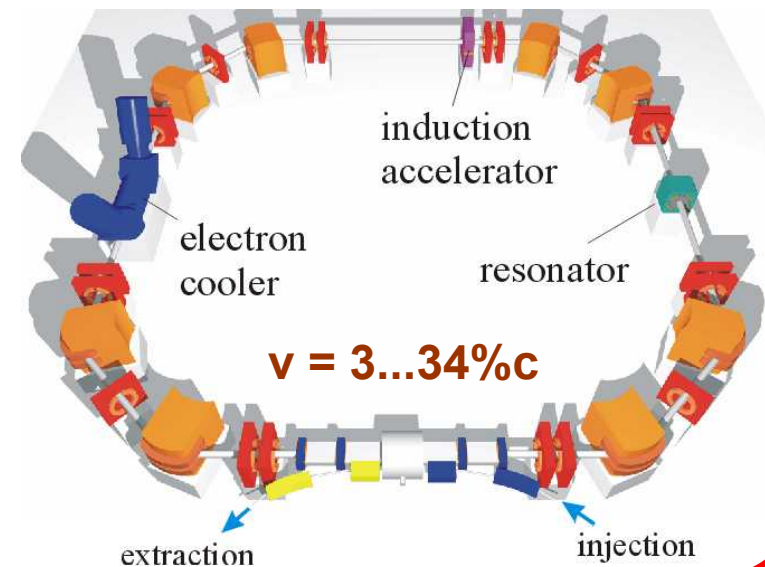
frequencies has to been known
very accurate

the higher the clock velocity,
the higher the sensitivity to $\delta\alpha$

Precision Spectroscopy



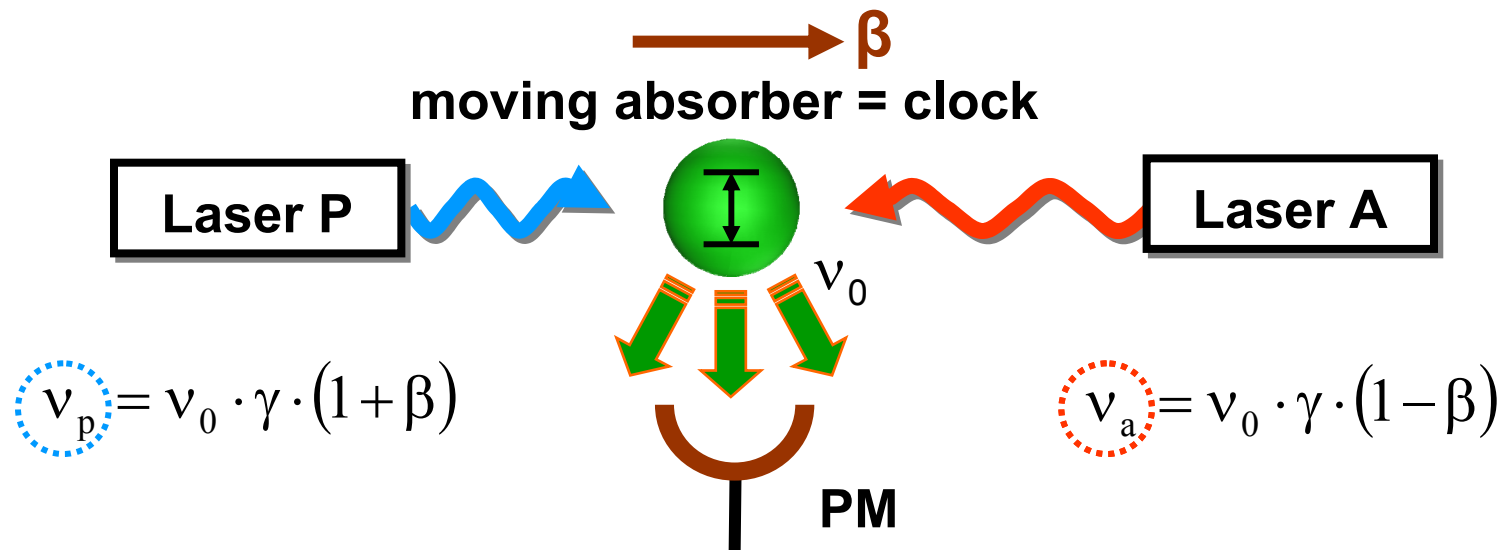
Storage Ring



Modern Ives-Stilwell experiment



Testing Lorentz transformation via measuring of the optical frequencies

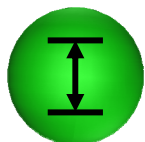


Testing time dilation via three optical frequencies

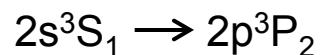
$$\frac{\nu_a \cdot \nu_p}{\nu_0^2} = \gamma^2 \cdot (1 - \beta^2) \stackrel{?}{=} 1 \quad \longrightarrow \quad \frac{\nu_a \cdot \nu_p}{\nu_0^2} = 1 + 2 \cdot \delta\alpha \cdot \beta^2$$



Helium-like lithium ion in the metastable triplet state



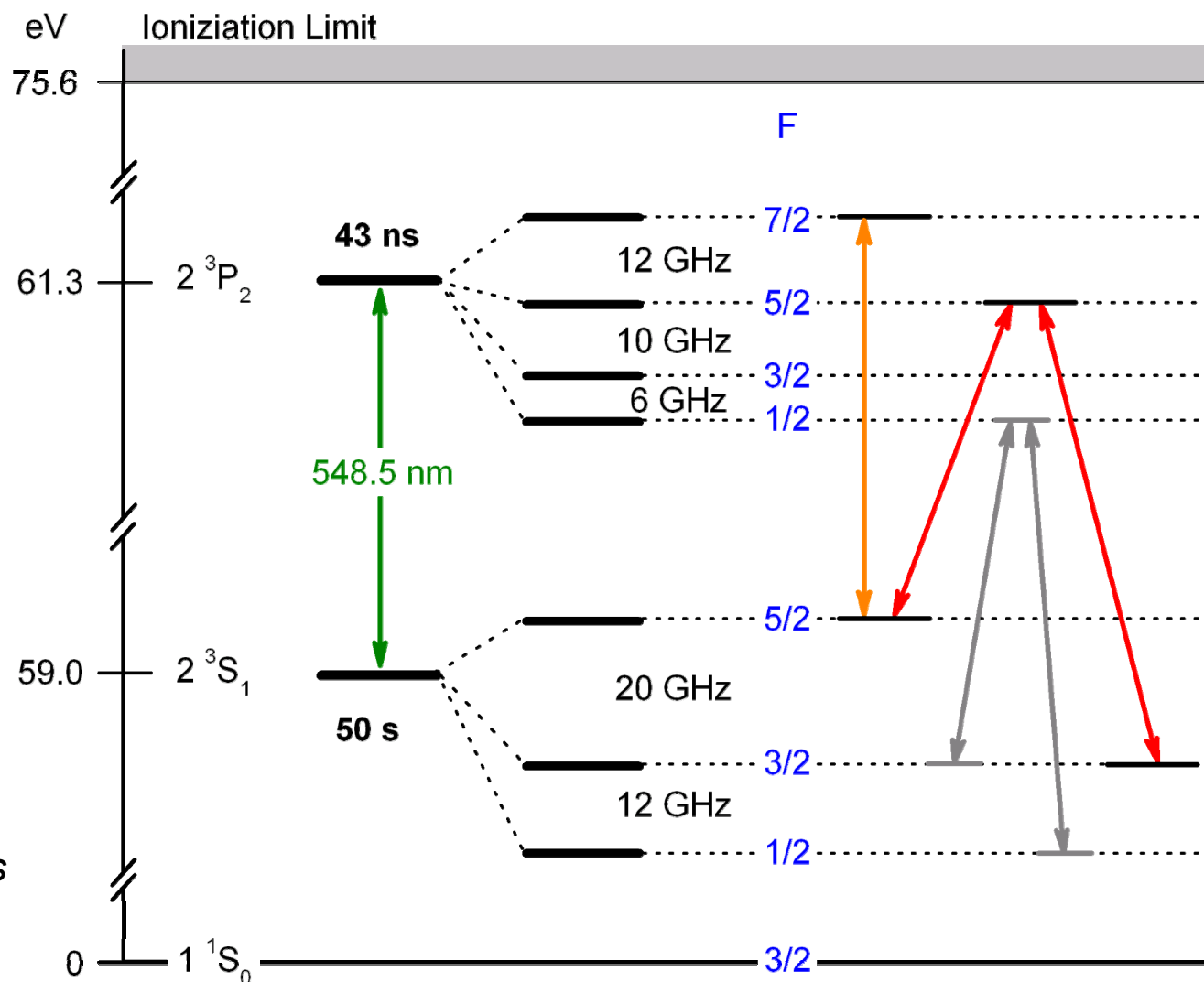
closed two level system



natural line width

3.7 MHz

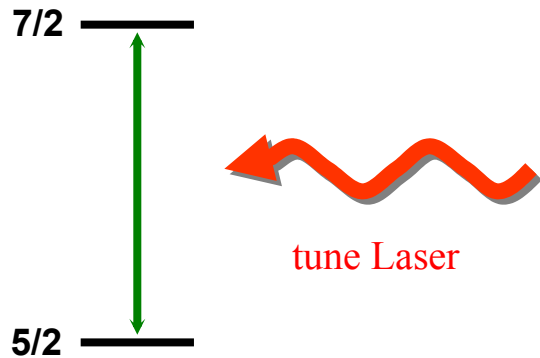
can be *accelerated* to and
stored at high velocities
with *superb beam qualities*



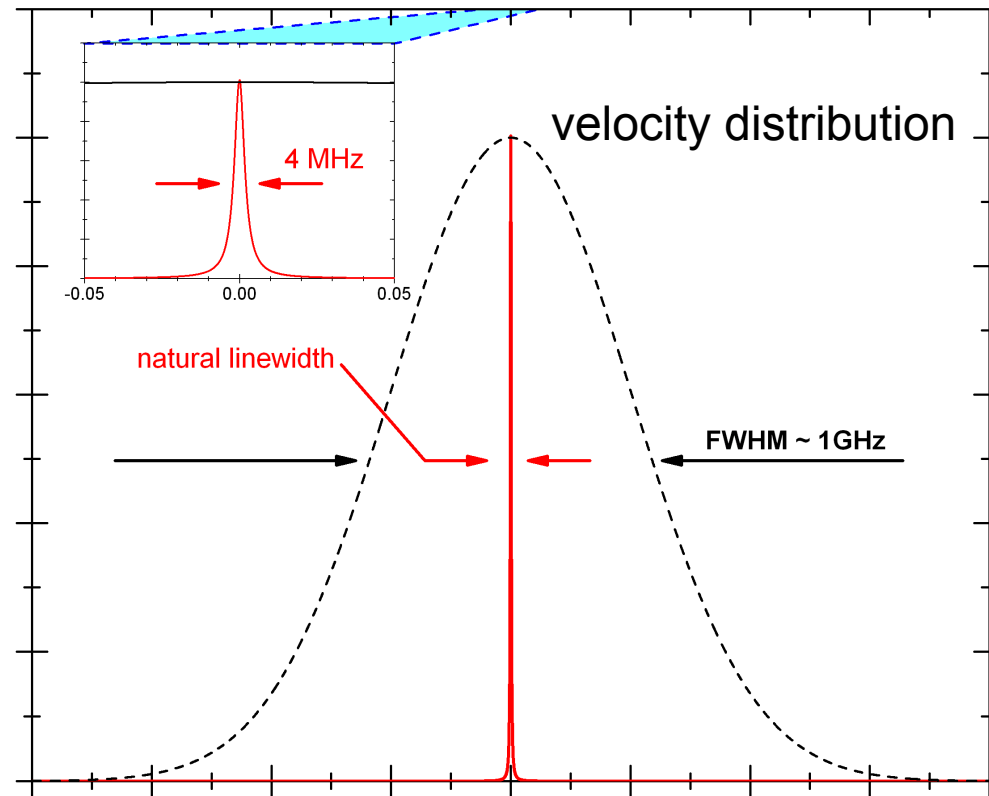
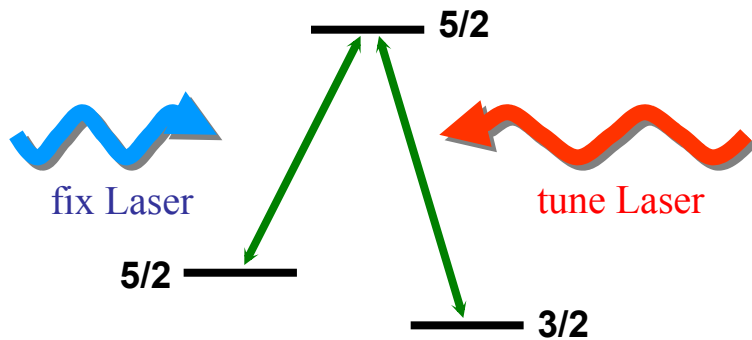
Spectroscopy in a storage ring



Doppler-broadened Spectroscopy



Λ - Spectroscopy

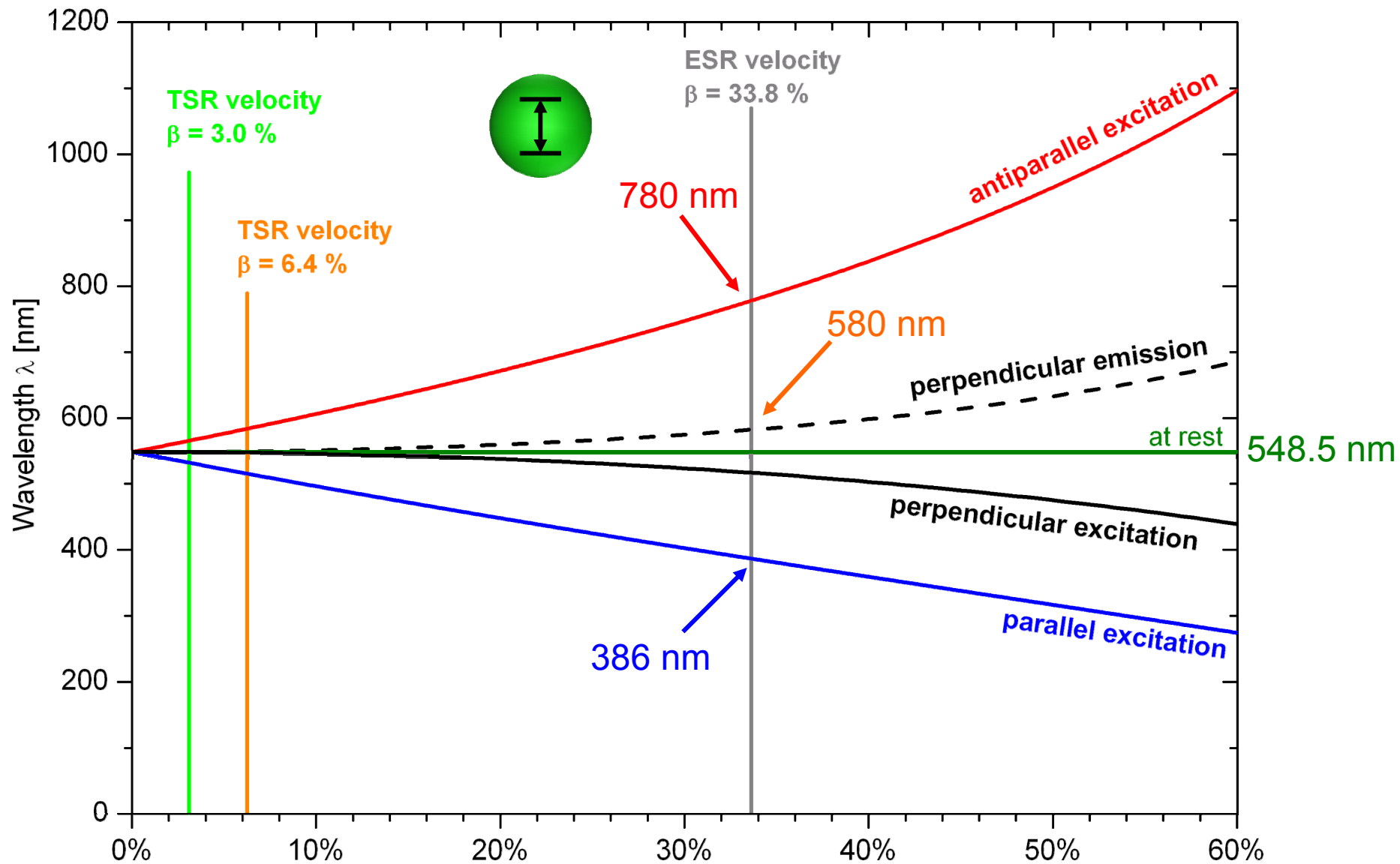


first-order Doppler-free peak

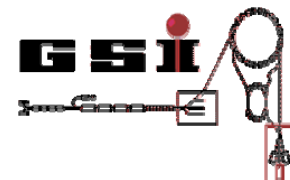
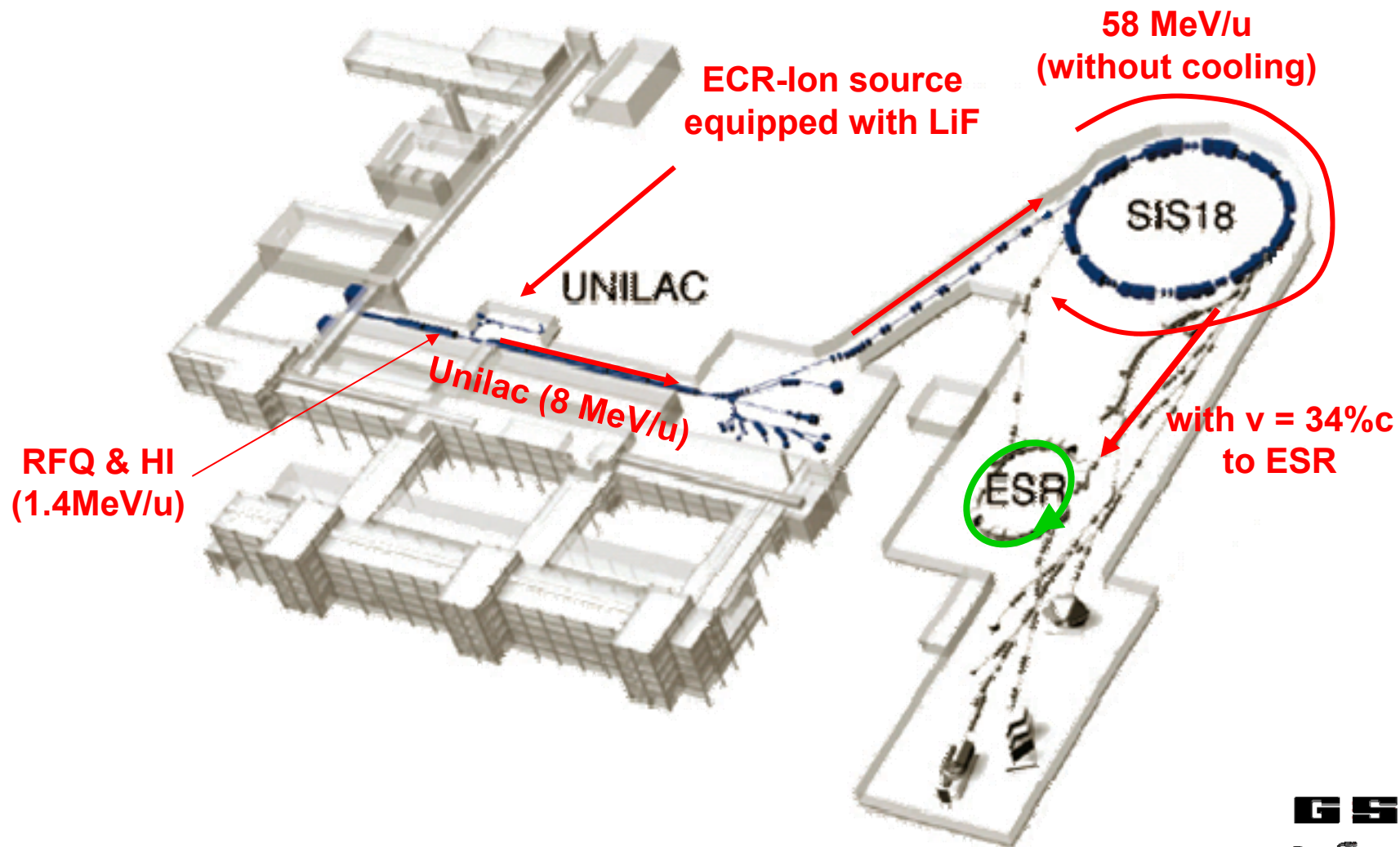
Both laser are in resonance with the same velocity group β_0

$$v_a \cdot v_p = v_1 \cdot v_2$$

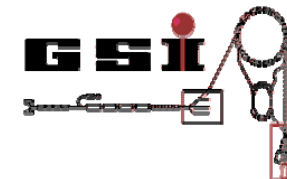
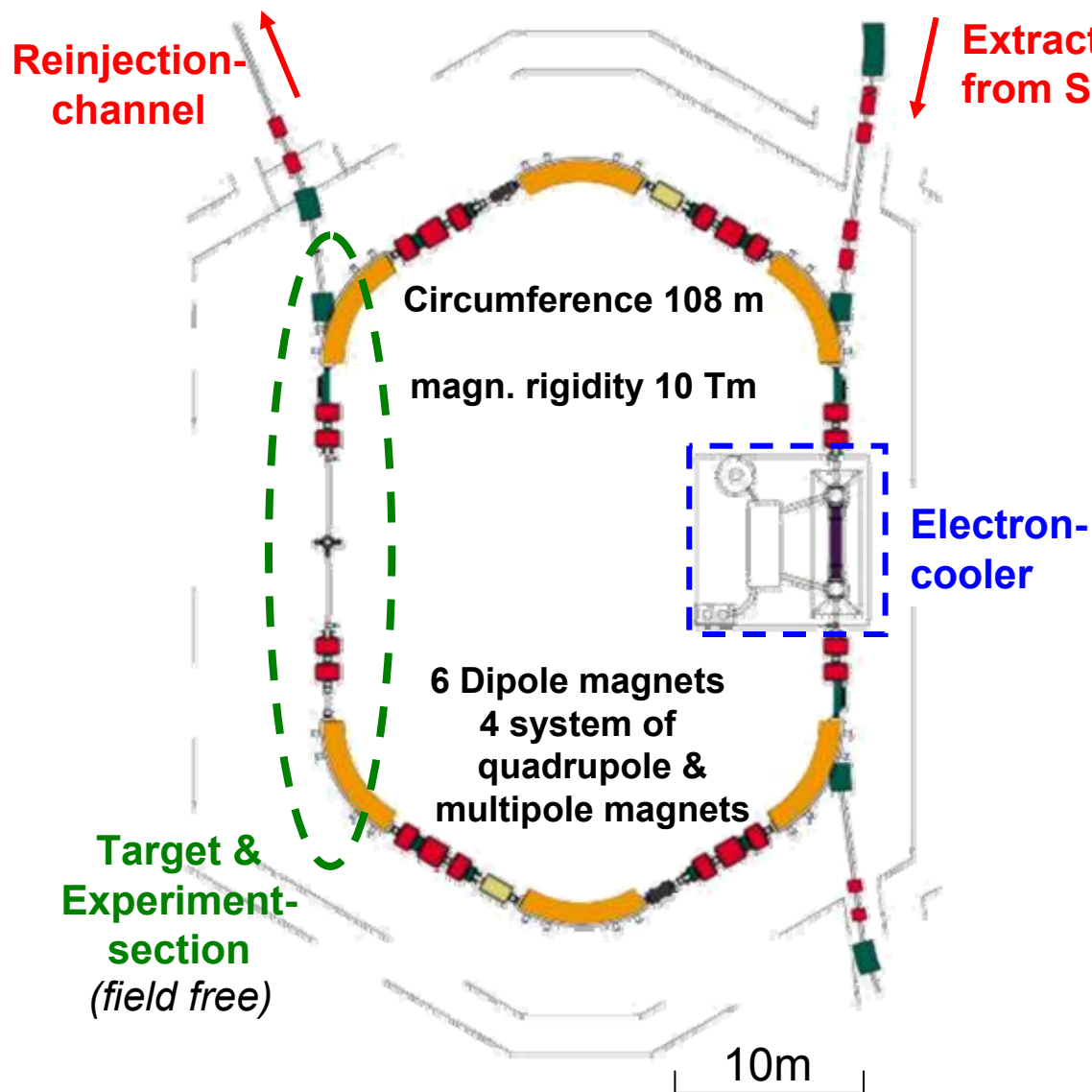
(High) relativistic ${}^7\text{Li}^+$



The GSI facility



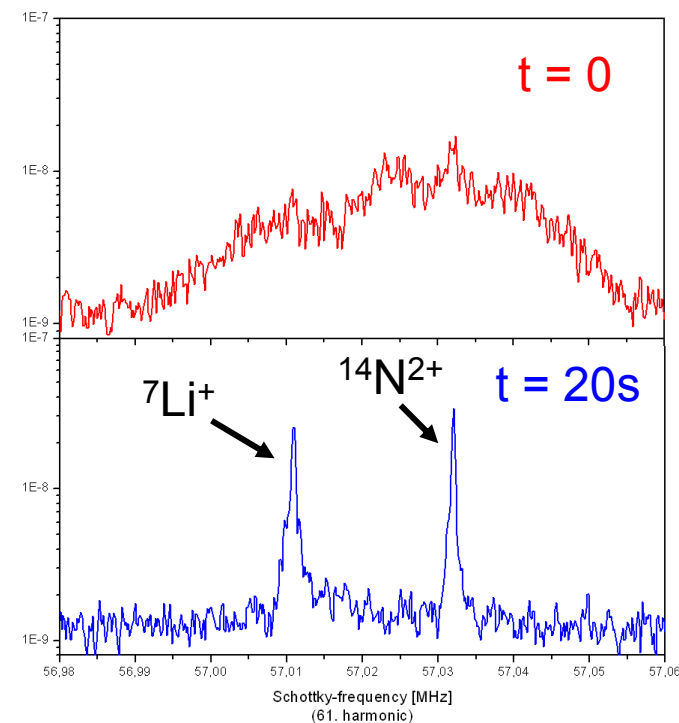
The experimental storage ring ESR



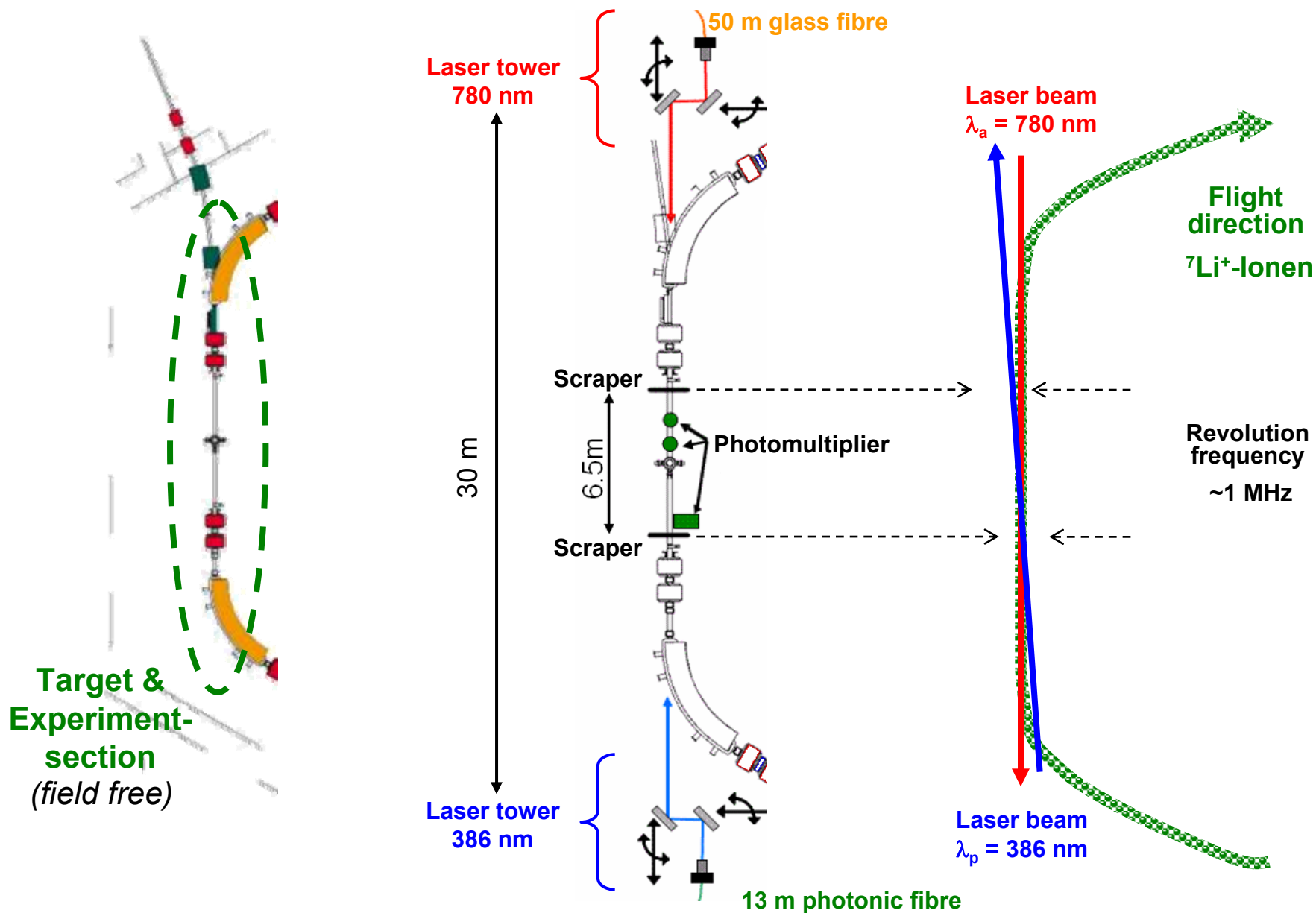
Ion current $\sim 25 \mu\text{A}$ 2×10^8 Ions

Ion beam storage time $\tau = 20 \text{ s} \dots 3 \text{ min}$

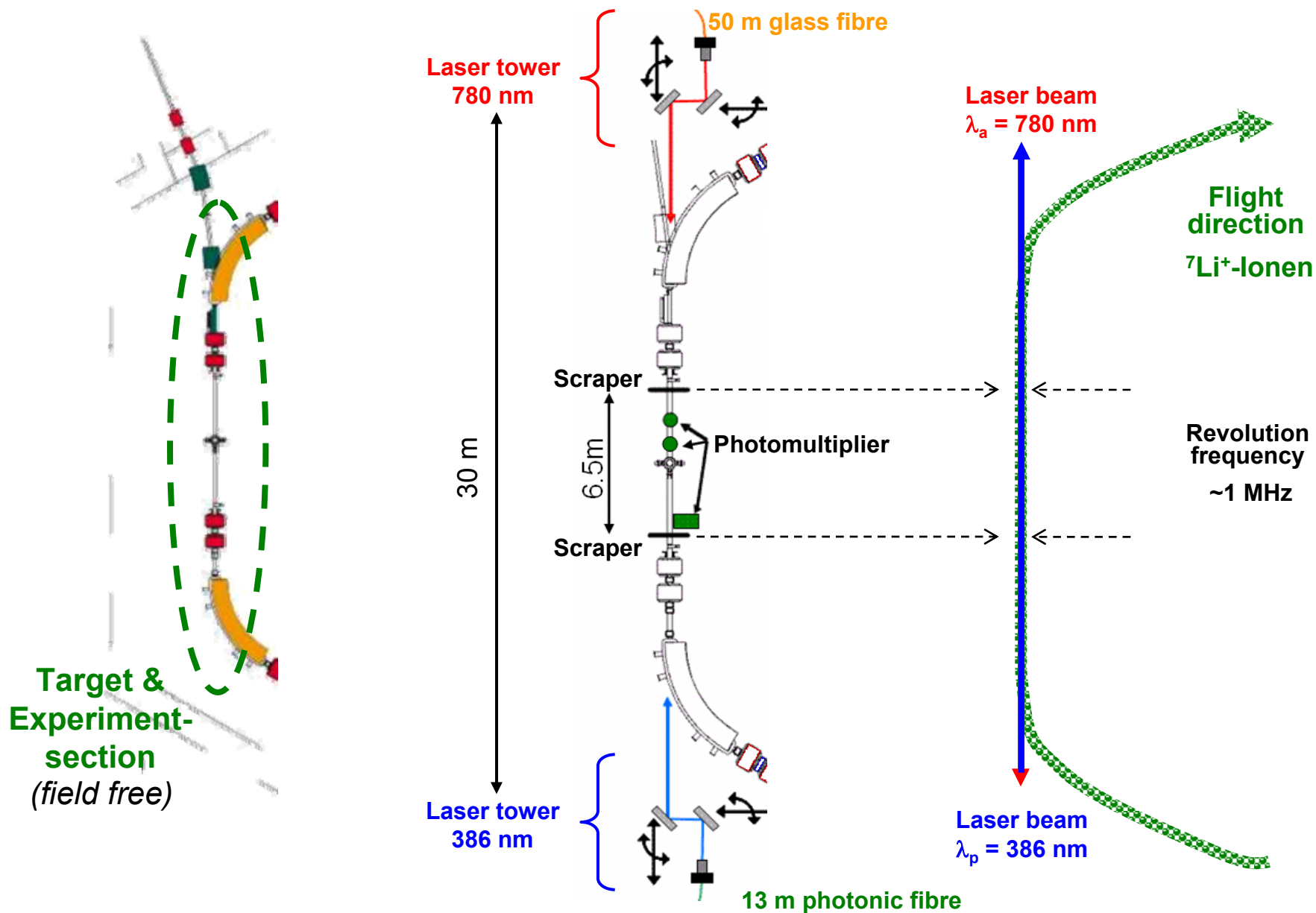
Momentum spread $\Delta p/p \sim 10^{-6}$



Experimental section



Experimental section



Laser system (simplified)

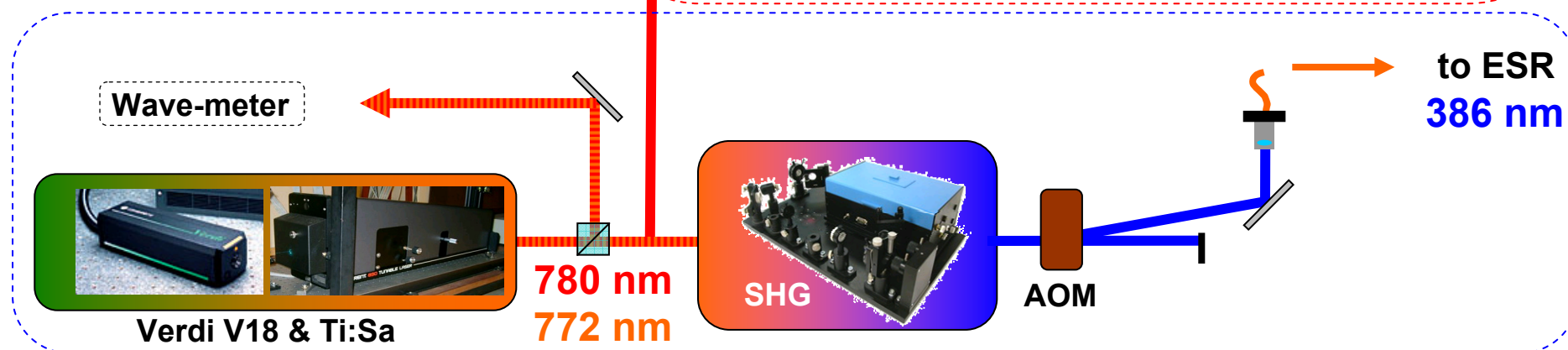
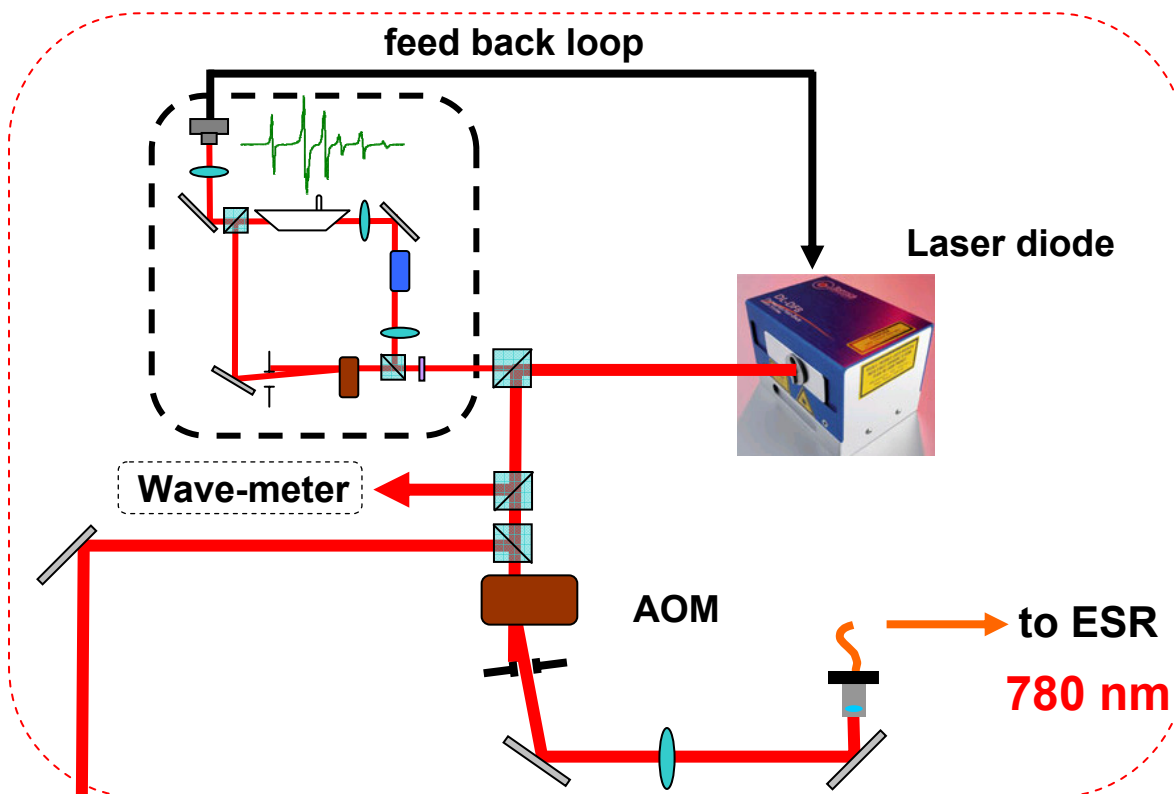


antiparallel excitation

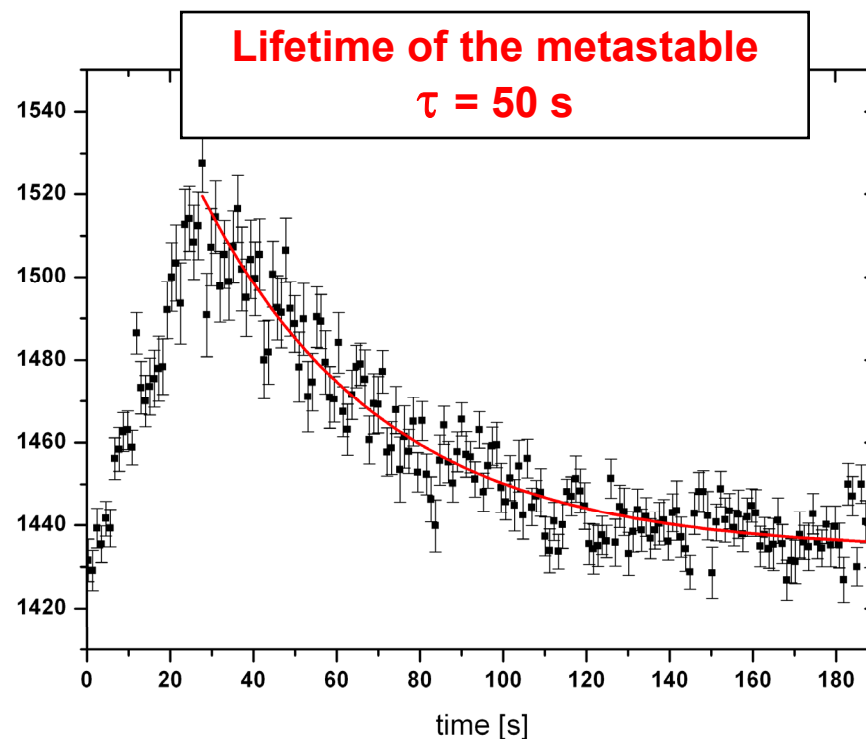
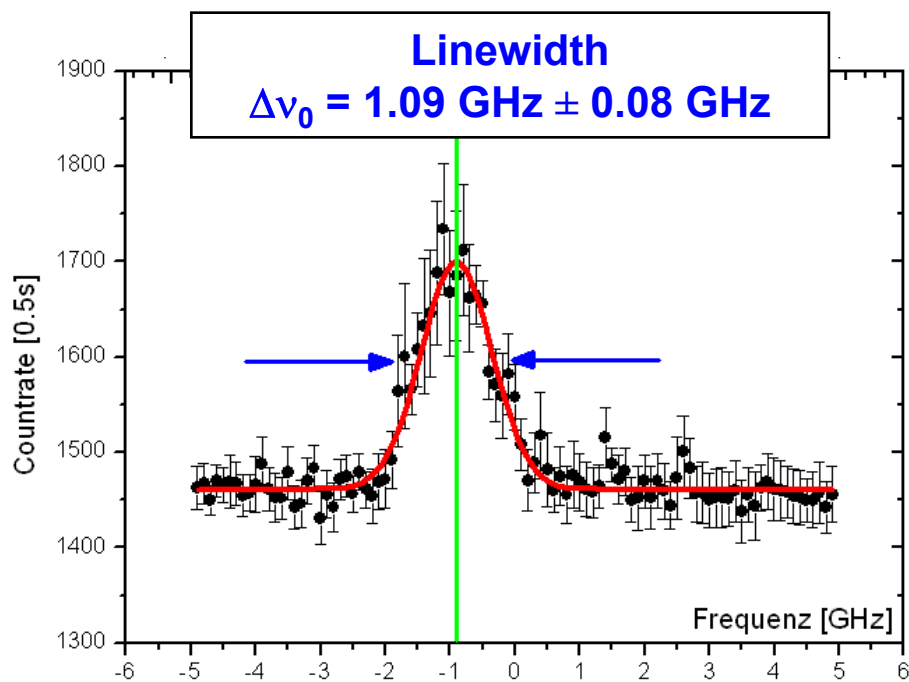
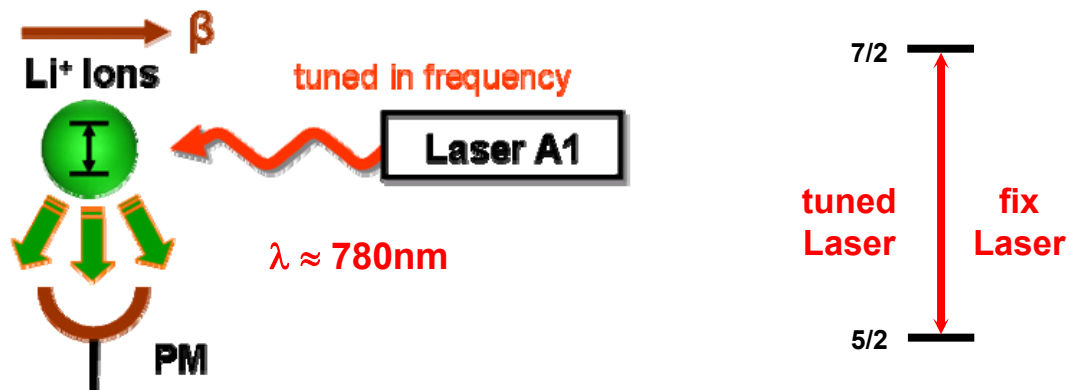
frequency reference
on rubidium via
fm-saturation spectroscopy
(< 1 MHz)

parallel excitation

frequency reference
wave meter (~ 100 MHz)
(more accurate reference tested but not
applied in beam time yet)

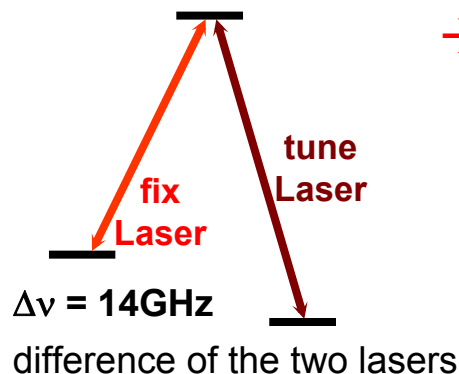


Characteristics of the metastable ${}^7\text{Li}^+$



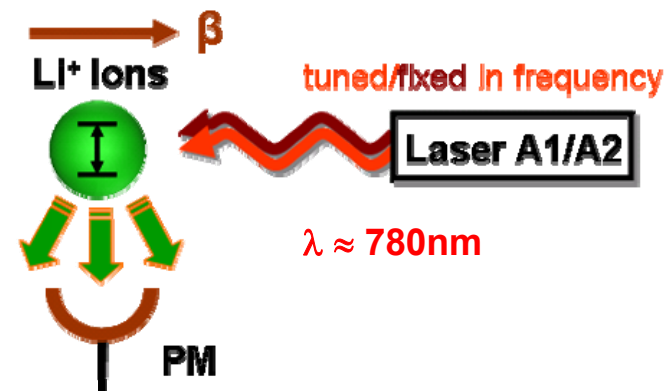
[C. Novotny et al., Hyperfine Interact. 171 (2006) 57]

Parallel lambda spectroscopy

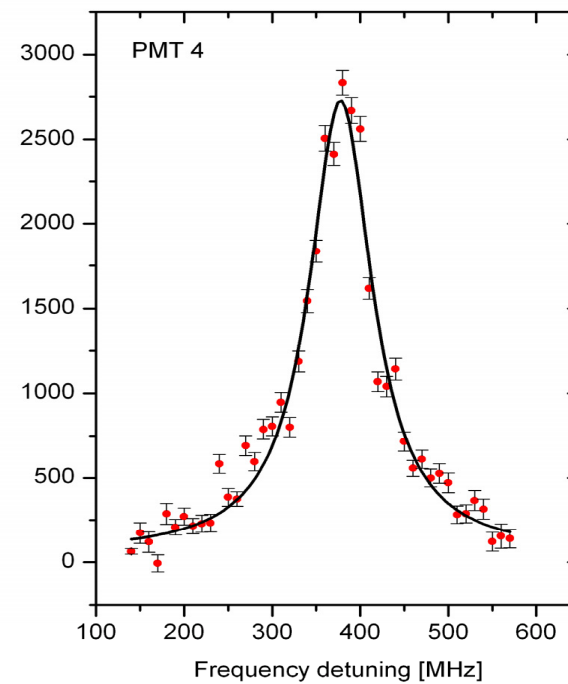
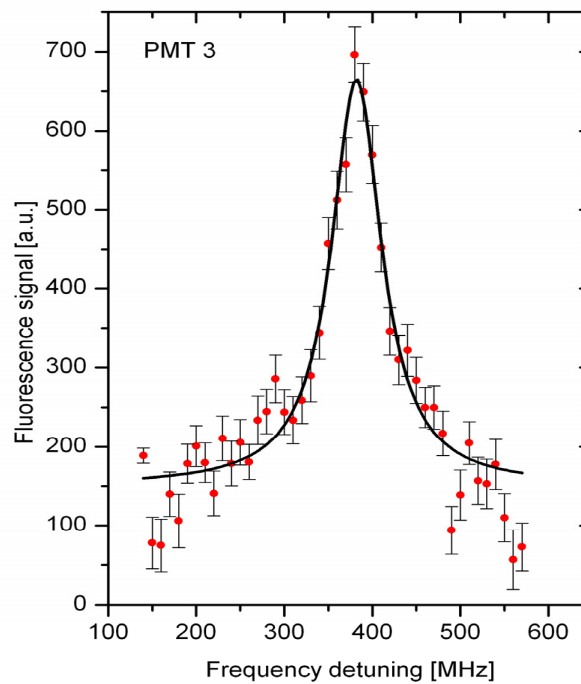


→ two “red” lasers :

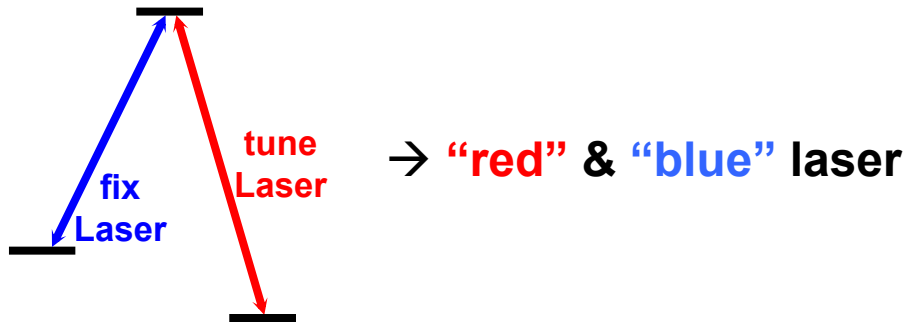
*first-order Doppler-free spectroscopy:
linewidth: (70...126) MHz
(10 times wider than the natural one)*



- both lasers from one site
(through one fiber)
- no uncertainty in
laser-laser alignment
- less background
- higher signal (less filters)



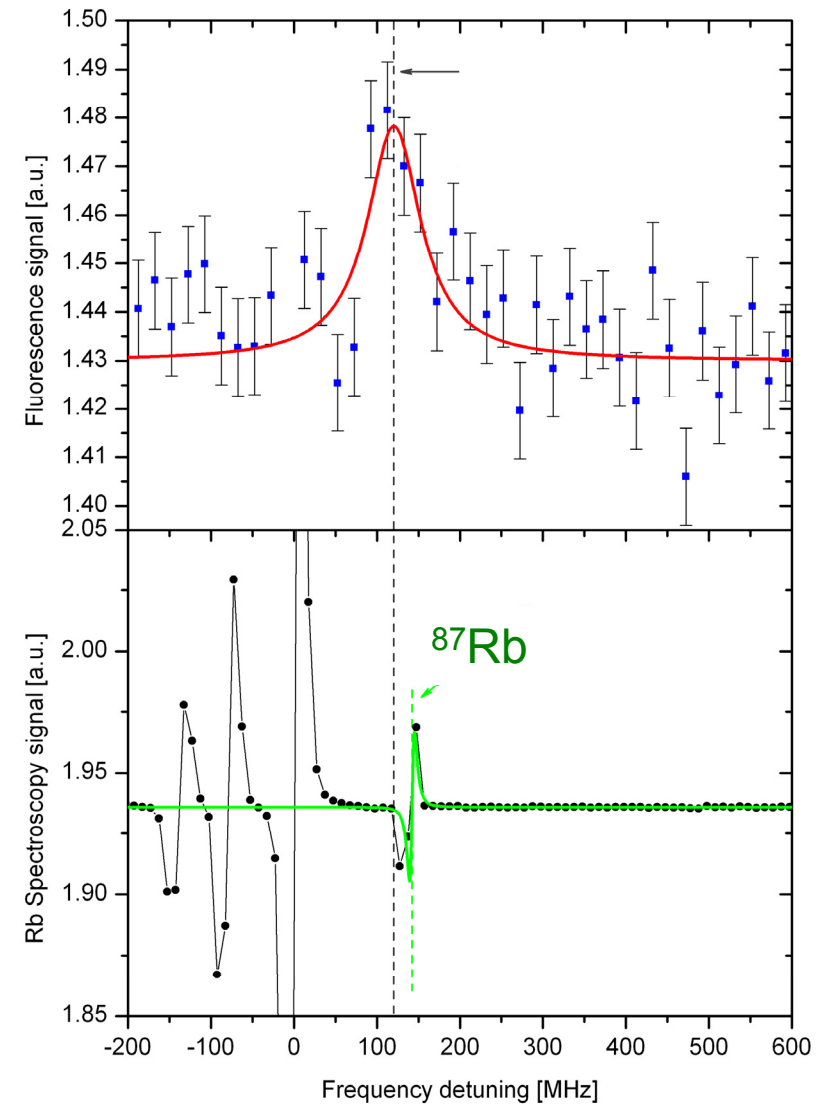
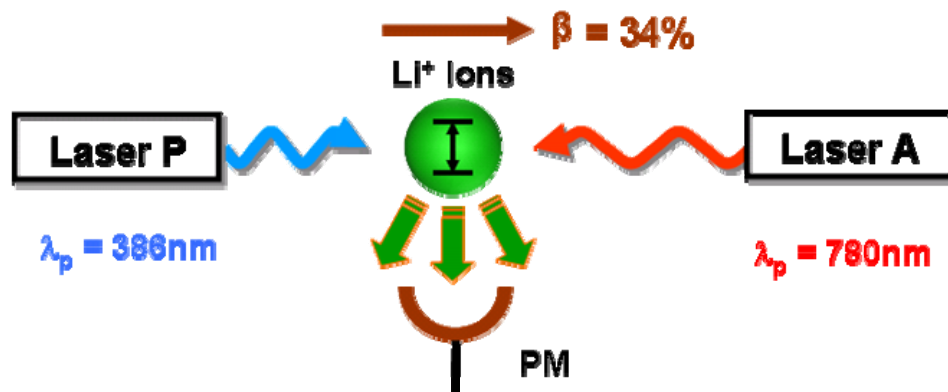
Antiparallel lambda spectroscopy



$$\Delta\nu = 79 \pm 25 \text{ MHz (laboratory frame)}$$

$$\Delta\nu = 109 \pm 32 \text{ MHz (ion frame)}$$

Peak position: $\pm 10 \text{ MHz}$



Impact on the test parameter



Using TSR to fix $\delta\alpha$ and ESR for second order terms

$$\left| 2 \cdot \delta\alpha \cdot \beta^2 + (\delta\alpha + 2 \cdot \delta\alpha_2) \cdot \beta^4 \right| < \left(\frac{v_p \cdot v_a}{v_1 \cdot v_2} - 1 \right) = \underline{3 \times 10^{-7}}$$

$$\delta\alpha_{\text{TSR}} < 8.4 \times 10^{-8}$$

[S. Reinhardt, et al. Nature Physics 3 (2007) 861]

$$\Delta_{\text{ESR}}$$

$$|\delta\alpha_2| < 9 \times 10^{-6}$$

Improvement by factor of **28** compared to former upper limit measured on H^0 @ 84%*c*

[D.W. MacArthur et al., PRL 56 (1986) 282]

consequences for $\delta\alpha$

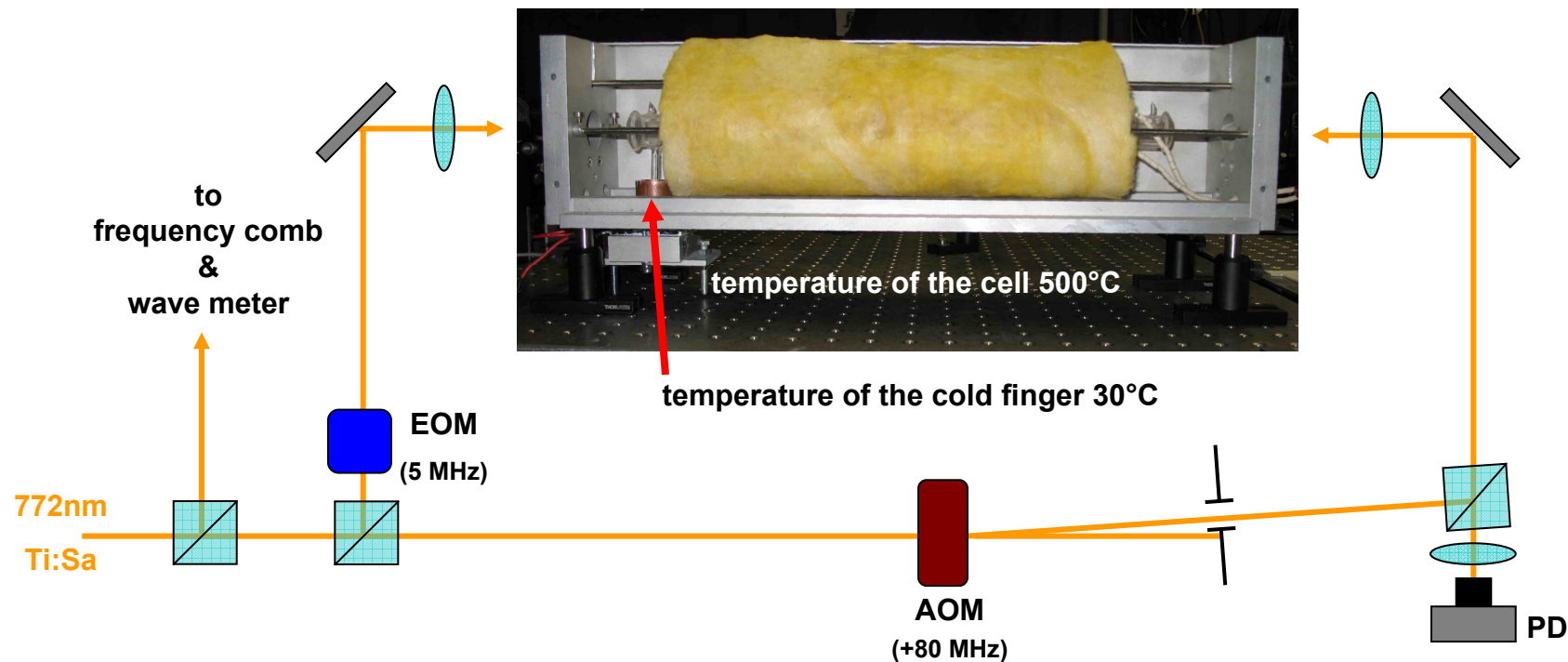
$$\frac{v_p \cdot v_a}{v_1 \cdot v_2} - 1 = 2 \cdot \delta\alpha \cdot \beta^2$$

$$\delta\alpha_{\text{ESR}} = (7 \pm 11) \times 10^{-7}$$

$$\delta\alpha_{\text{TSR}} = (4.8 \pm 8.4) \times 10^{-8}$$

$$\frac{\text{ESR}}{\text{TSR}} \approx 13$$

Iodine reference @ 772 nm



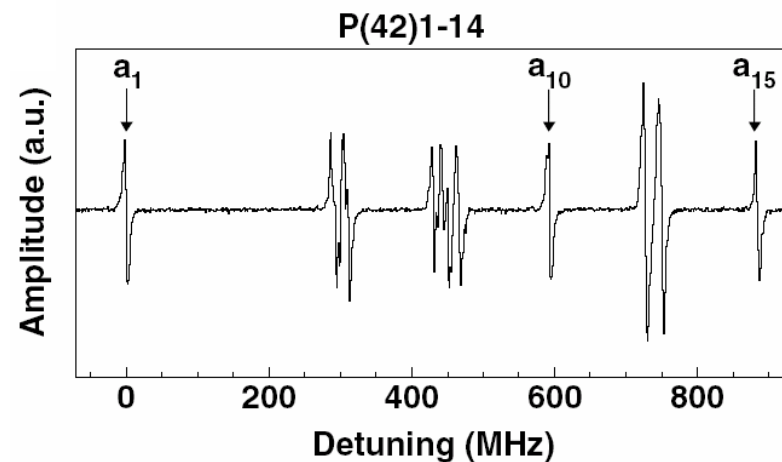
calibrated transition for the SRT experiment

P(42) 1-14 (772nm)

a_1 : $(388\,605\,083.71 \pm 0.30)$ MHz

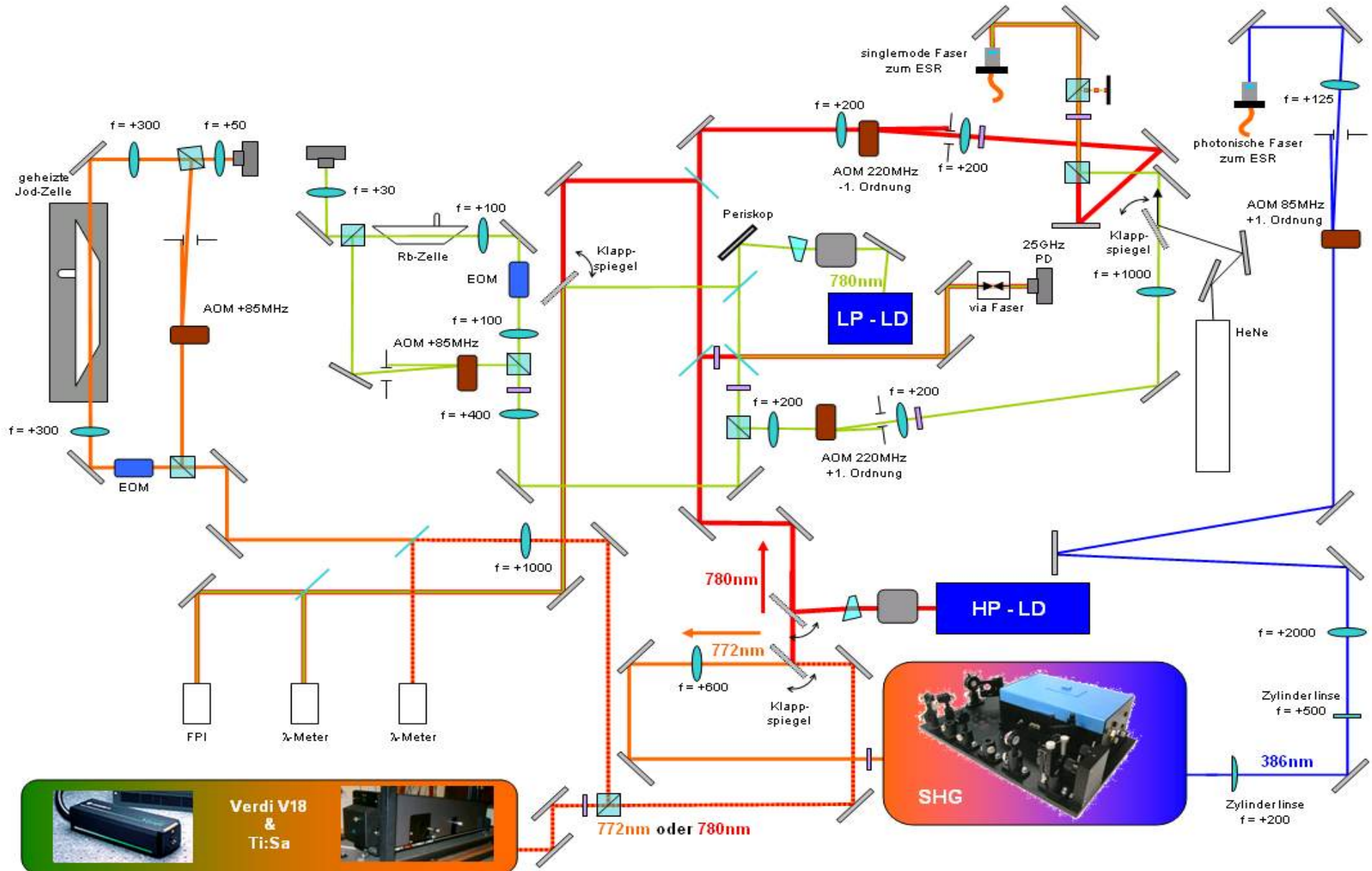
$|a_1 - a_{10}|$: $(587\,187 \pm 42)$ kHz

$|a_1 - a_{15}|$: $(881\,362 \pm 42)$ kHz



[S. Reinhardt et al., Opt. Com. **274** (2007) 354]

"Extended" laser system



Verdi V18 & Ti:Sa

Summary



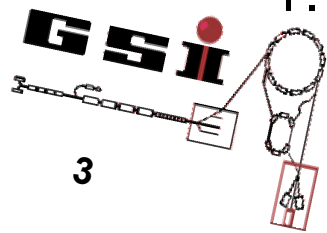
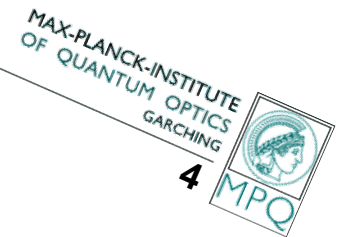
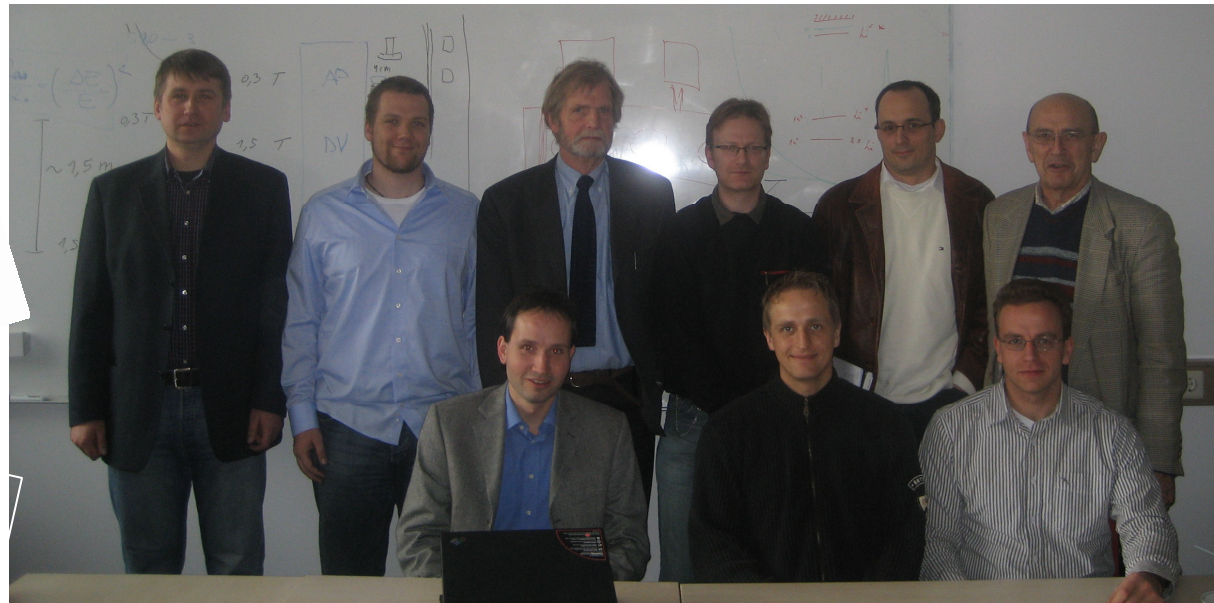
Presented :

- ✓ upper bound on test parameter $\alpha < 8 \times 10^{-8}$ (at TSR)
- ✓ the **possibility of precision spectroscopy** in high **relativistic ion beams**
- ✓ **improved upper limit** for second-order deviations by a **factor 28** (at ESR)
- ✓ the **feasibility** for a **new first-order upper limit**
- ✓ **calibration of iodine transitions** at 772 nm

Next steps :

- ☒ beam time with full frequency resolution ($\Delta \nu < 1$ MHz)
- ☒ systematic investigations (switching schemes, geometrical uncertainties, etc...)
- ☒ applying saturation spectroscopy

The SRT-Collaboration



C. Novotny¹, **S. Reinhardt**^{2,4}, **S. Karpuk**¹,
B. Bernhardt⁴, **D. Bing**², **G. Ewald**³, **C. Geppert**², **G. Gwinner**⁵,
T. W. Hänsch⁴, **R. Holzwarth**⁴, **G. Huber**¹, **H.-J. Kluge**³,
T. Kühl^{1,3}, **W. Nörtershäuser**^{1,3}, **G. Saathoff**^{2,4},
D. Schwalm², **T. Stöhlker**³, **T. Udem**⁴, **A. Wolf**²