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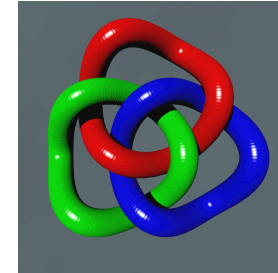
A U.S. Department of Energy laboratory  
managed by UChicago Argonne, LLC

# *Precision Laser Spectroscopy of Exotic Helium Isotopes*

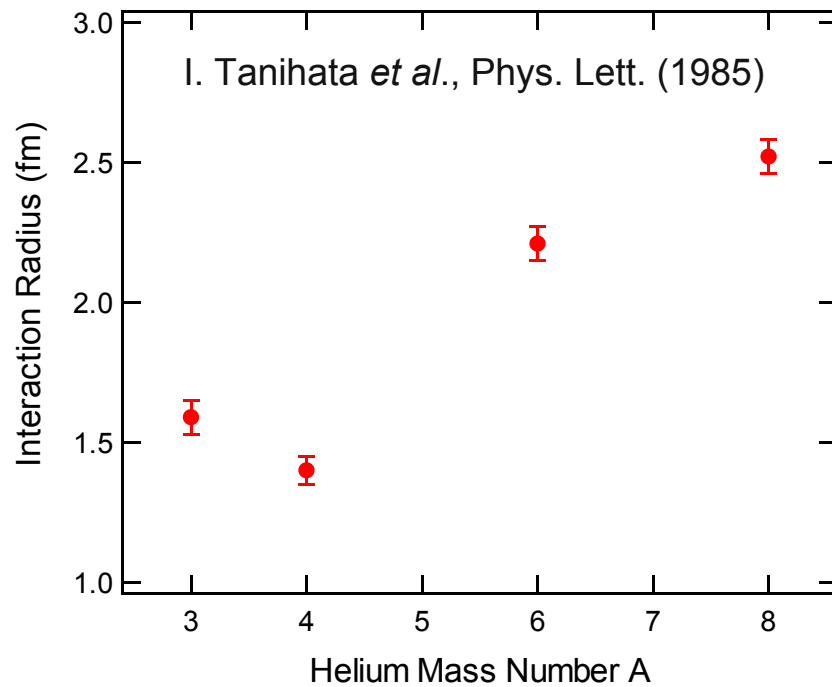
*Peter Müller*

# Neutron Halo Nuclei ${}^6\text{He}$ and ${}^8\text{He}$

Isotope	Half-life	Spin	Isospin	Core + Valence
He-6	807 ms	$0^+$	1	$\alpha + 2n$
He-8	119 ms	$0^+$	2	$\alpha + 4n$



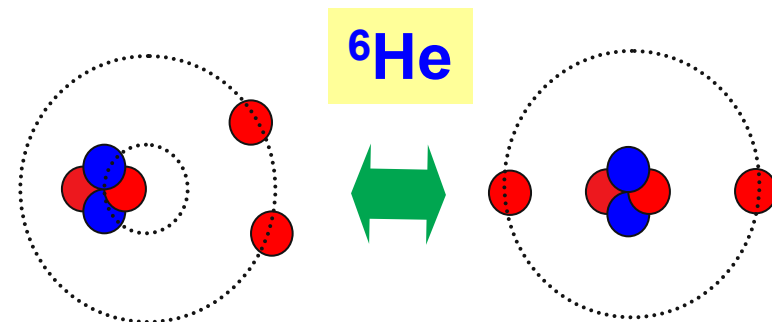
Borromean



## Core-Halo Structure

$$\sigma_I(6\text{He}) - \sigma_I(4\text{He}) = \sigma_{-2n}(6\text{He})$$

I. Tanihata *et al.*, Phys. Lett. (1992)



## Effective Model of Nuclear Interaction

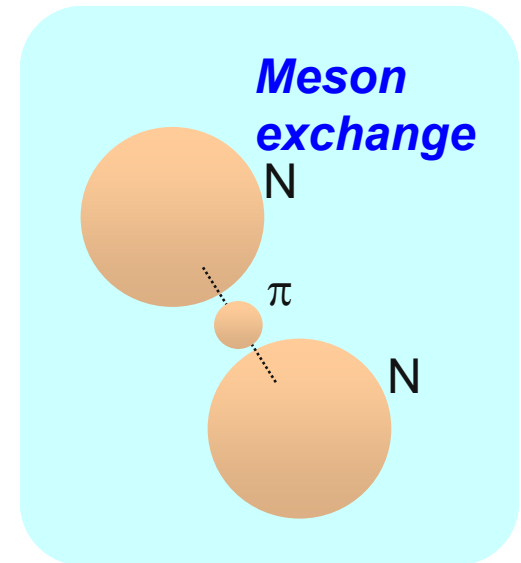
### Two-body potential: *Argonne V18*

$$H = \sum_i K_i + \sum_{i < j} v_{ij}^{\gamma} + v_{ij}^{\pi} + v_{ij}^R$$

EM
1- $\pi$ 
short-range

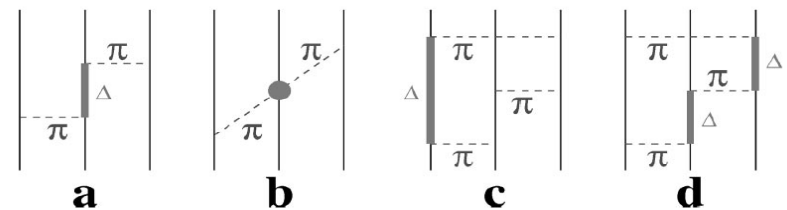
Coupling parameters fit to NN scattering data

Problem: binding energy of most light nuclei too small



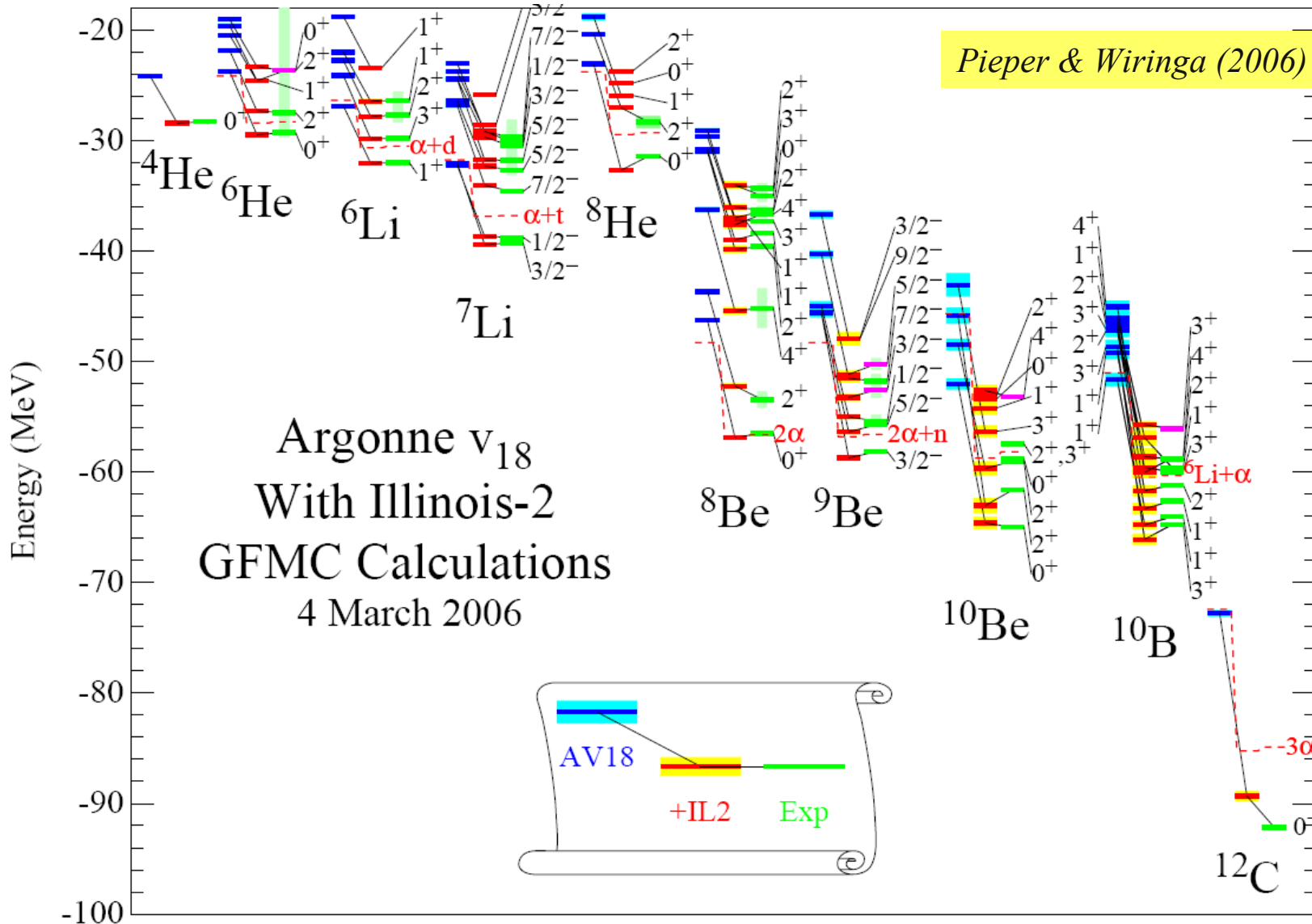
### Three-body potential: *Illinois-2*

$$V_{ijk} = V_{ijk}^{2\pi} + V_{ijk}^{3\pi} + V_{ijk}^R$$

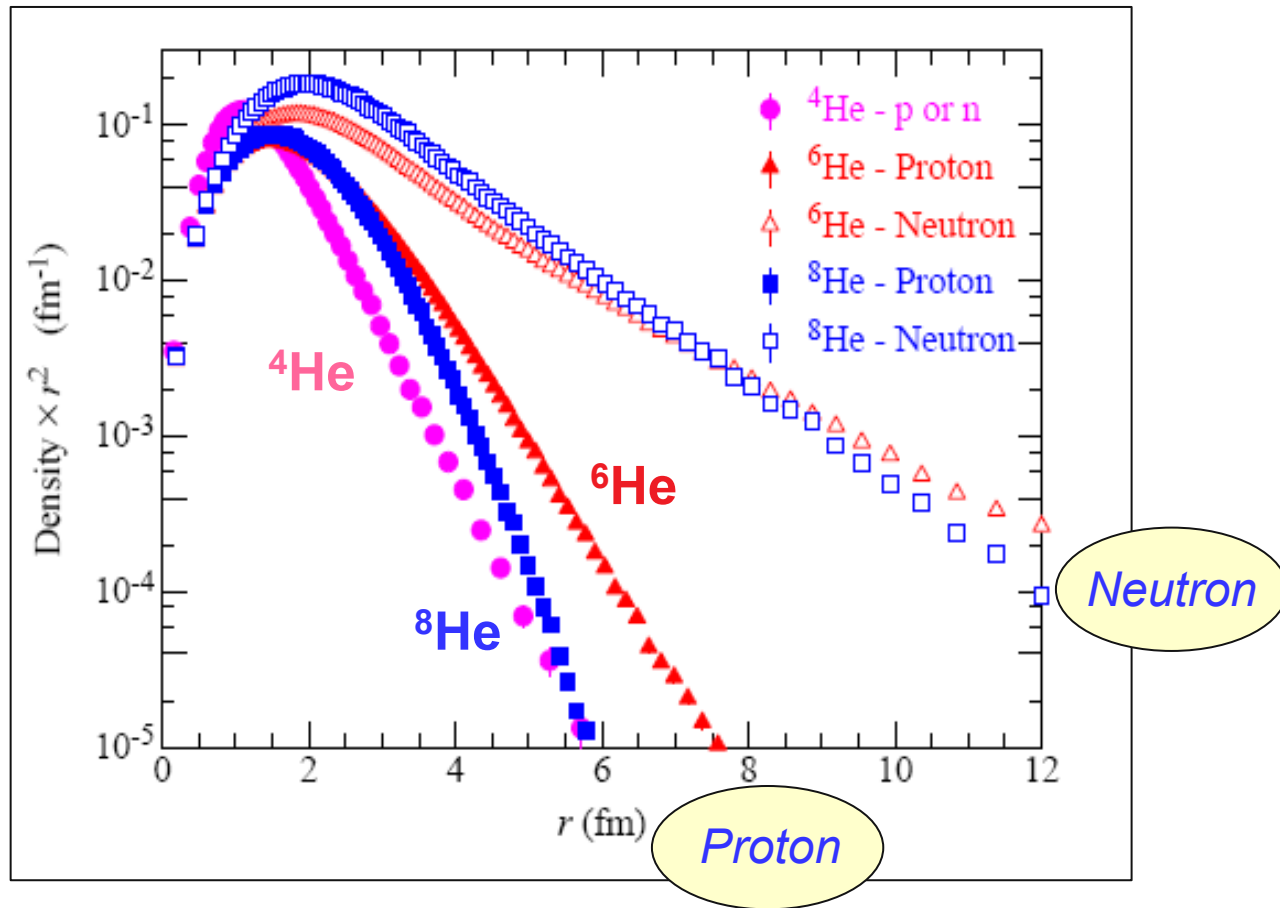


Coupling parameters fit to energy levels of light nuclei

# Green's Function Monte Carlo Calculations

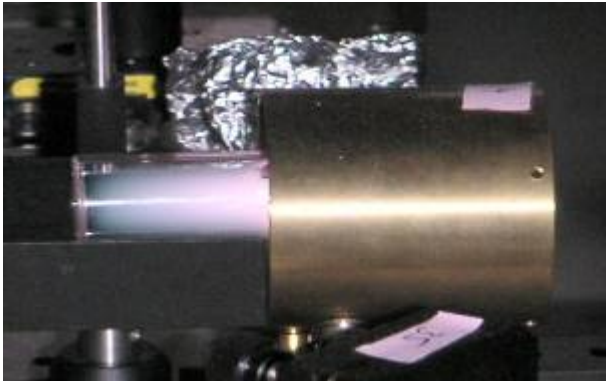


# GFMC – Neutron and Proton Densities in Helium-4,6,8

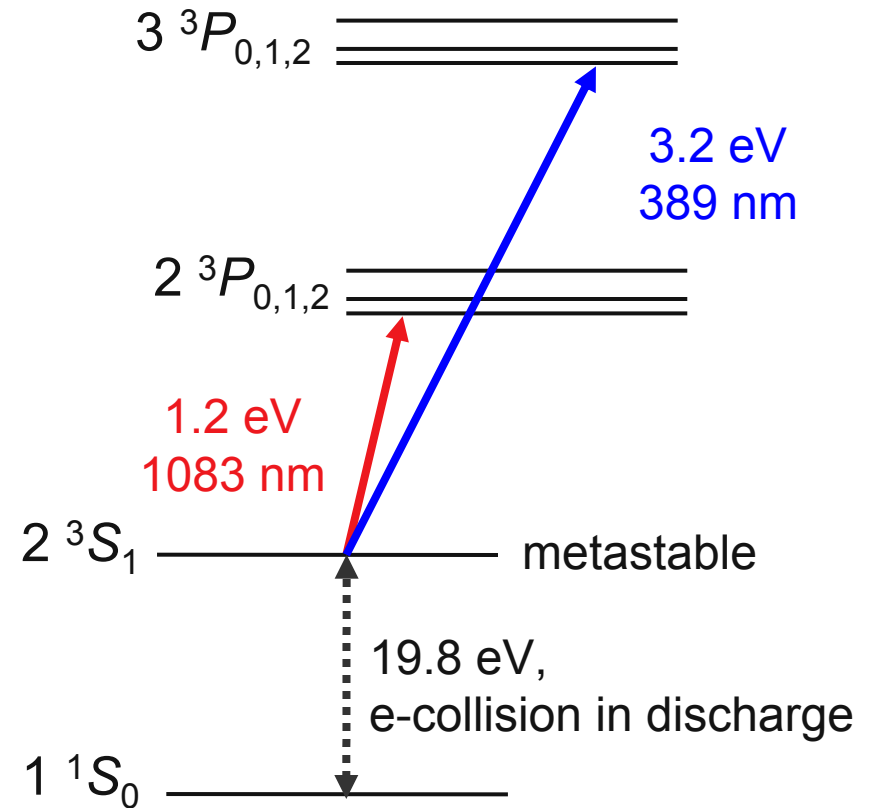


# Atomic Energy Levels of Helium

He discharge



He energy level diagram

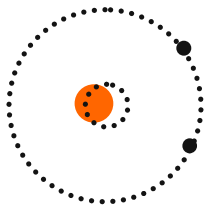


# Atomic Isotope Shift

Isotope Shift  $\delta\nu = \delta\nu_{MS} + \delta\nu_{FS}$

Mass shift:

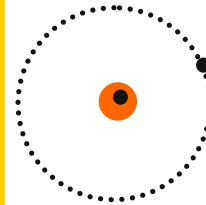
due to nucleus recoil



$$\delta\nu_{MS} \propto \frac{A - A'}{AA'}$$

Field shift:

due to nucleus size



$$\delta\nu_{FS} \propto Z \times \Delta[\Psi(0)]^2 \times \delta\langle r^2 \rangle$$

For  $2^3S_1 - 3^3P_2$  transition @ 389 nm:

$$\delta\nu = \delta\nu_{MS} + C_{FS} \delta\langle r^2 \rangle$$

$${}^6\text{He} - {}^4\text{He} : \delta\nu_{6,4} = 43196.202(16) \text{ MHz} + 1.008 (\langle r^2 \rangle_{\text{He4}} - \langle r^2 \rangle_{\text{He6}}) \text{ MHz/fm}^2$$

$${}^8\text{He} - {}^4\text{He} : \delta\nu_{8,4} = 64702.519(1) \text{ MHz} + 1.008 (\langle r^2 \rangle_{\text{He4}} - \langle r^2 \rangle_{\text{He8}}) \text{ MHz/fm}^2$$

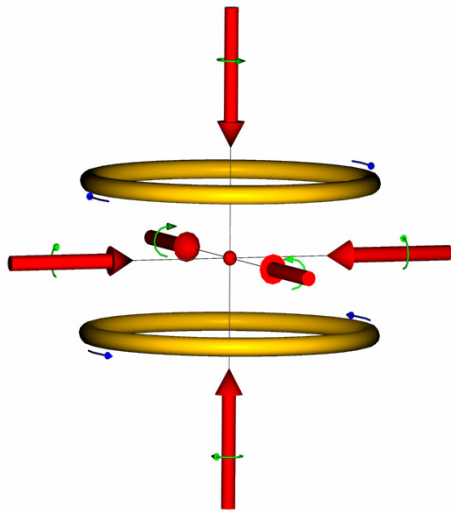
G.W.F. Drake, Univ. of Windsor, *Nucl. Phys. A737c*, 25 (2004)

**100 kHz error in IS  $\leftrightarrow$  ~ 1% error in radius**

# Laser Cooling and Trapping

Technical challenges:

- Short lifetime, small samples ( $<10^6$  atoms/s available)
- Low metastable population efficiency ( $\sim$  one in 100.000)
- Precision requirement (100 kHz = Doppler shift @ 4 cm/s )



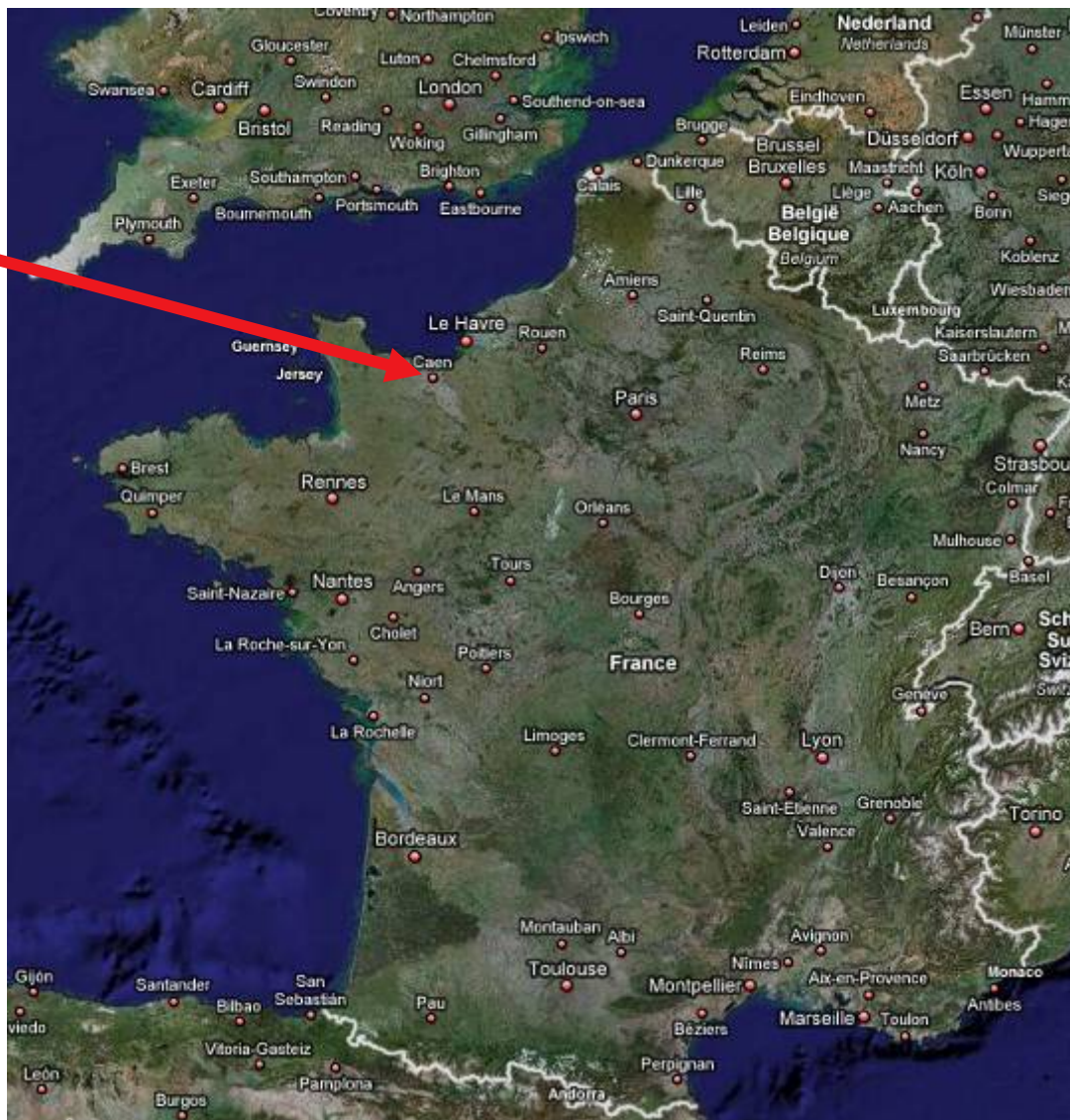
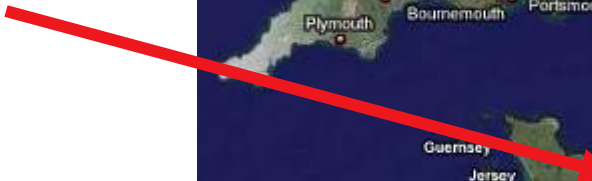
## Magneto-Optical Trap (MOT)

- **Cooling:** Temperature  $\sim$  1 mK,  
→ avoid Doppler shift / width
- **Long observation time:** 100 ms
- **Spatial confinement:** trap size  $<$  1 mm  
→ single atom sensitivity
- **Selectivity:** → no isotopic / isobaric interference



# Where to find $^8\text{He}$ ?

**GANIL**  
Caen, France

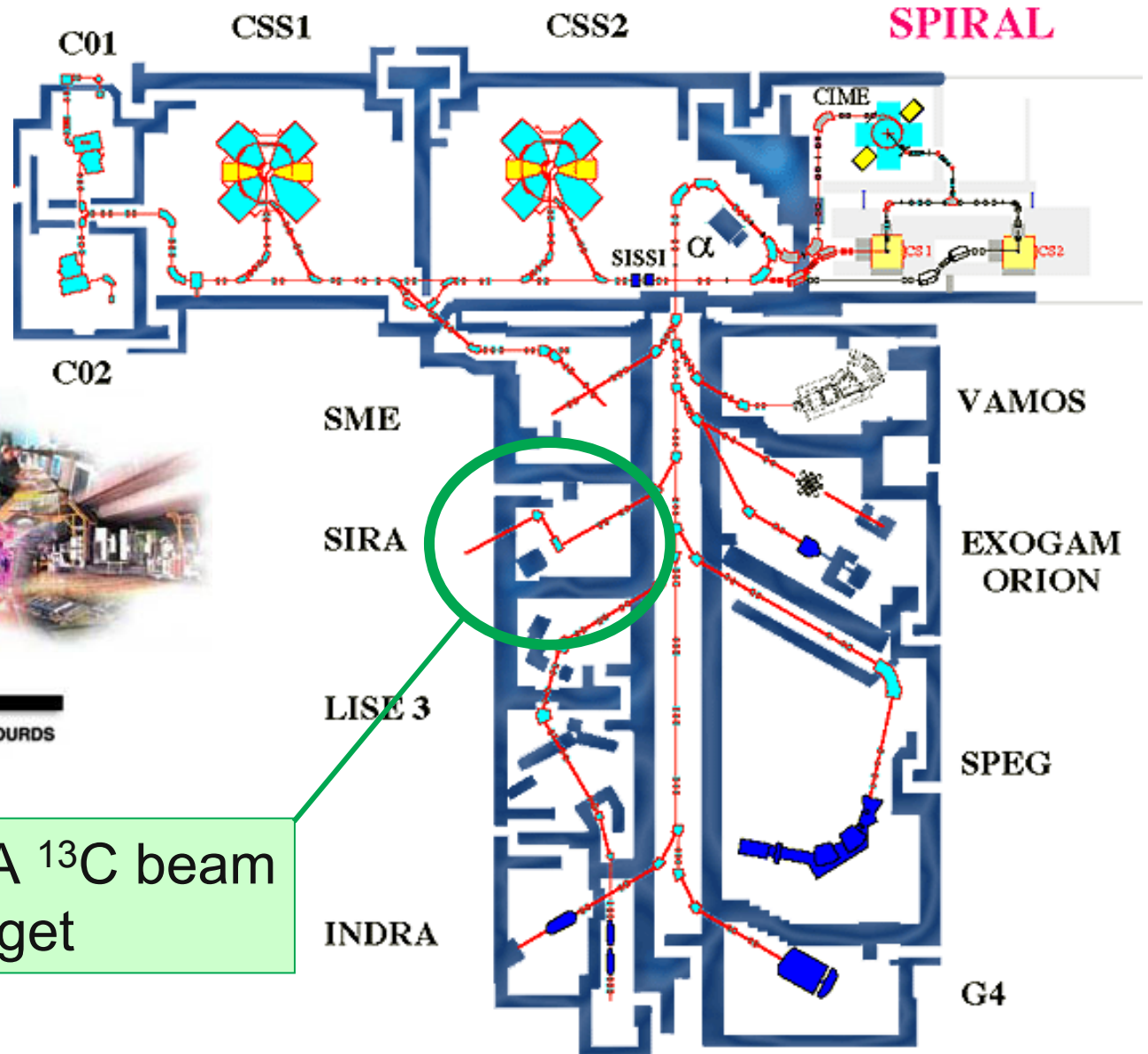


# He-8 @ GANIL

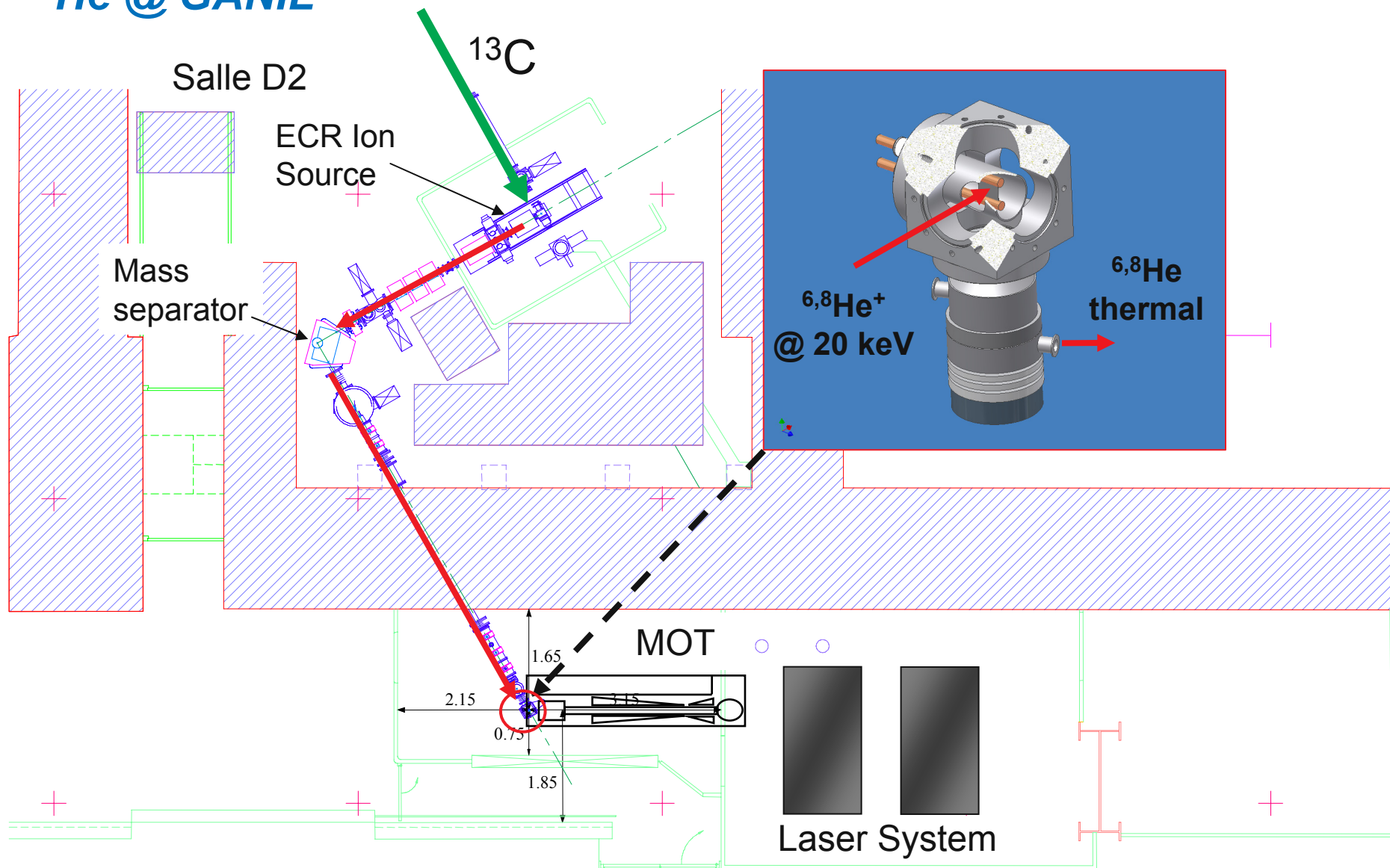


**GANIL**  
GRAND ACCELERATEUR NATIONAL D'IONS LOURDS  
LABORATOIRE COMMUN DSM/CEA-IN2P3/CNRS

75 MeV/u, 0.4 pμA <sup>13</sup>C beam  
on <sup>12</sup>C target



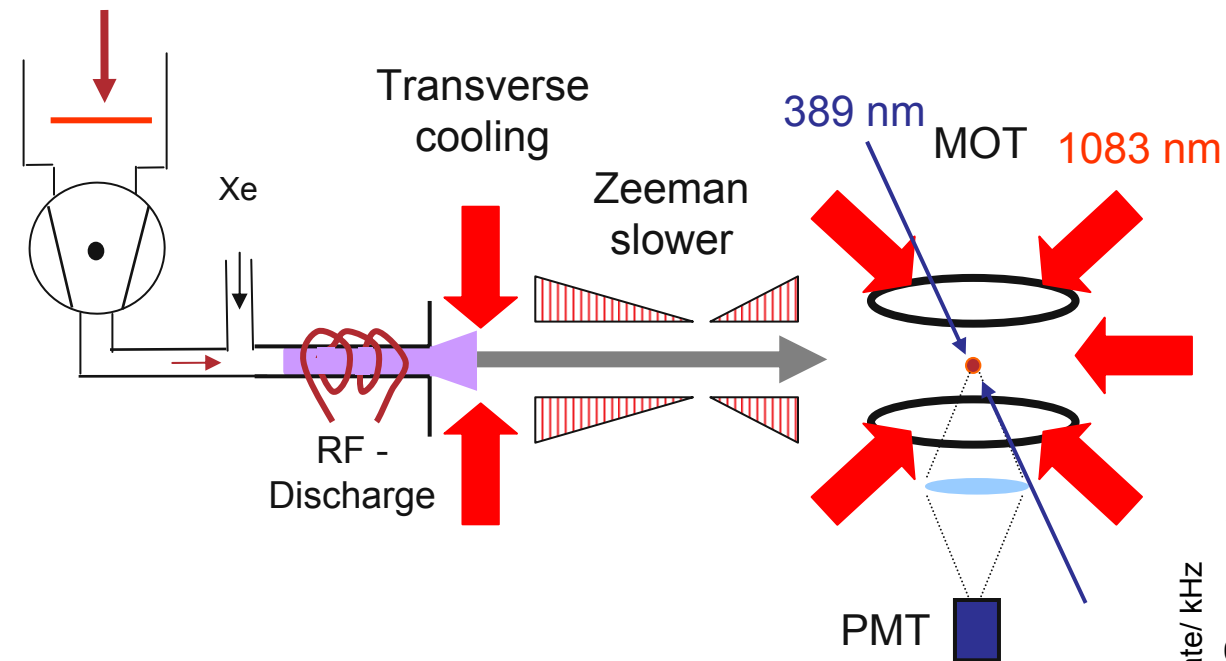
# $^8\text{He}$ @ GANIL



# Atom Trapping of ${}^6\text{He}$ & ${}^8\text{He}$ at GANIL

$\sim 1 \times 10^8$   ${}^6\text{He}^+/\text{s}$   
 $\sim 5 \times 10^5$   ${}^8\text{He}^+/\text{s}$

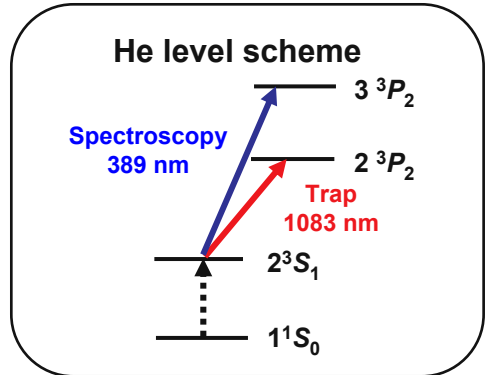
## Atom Trap Setup



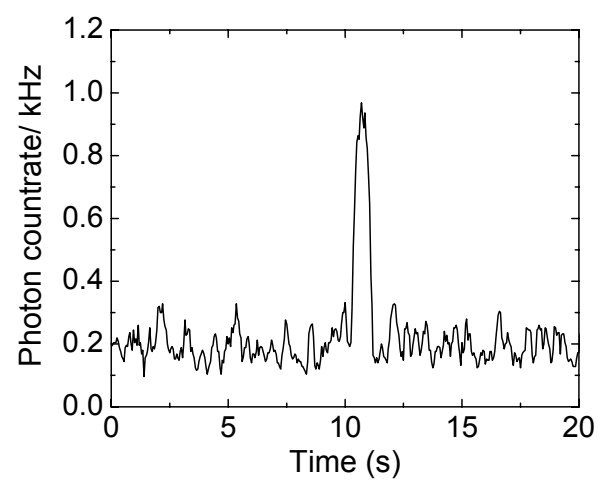
Source  
 $\sim 5 \times 10^7$  He-6/s,  
 $\sim 1 \times 10^5$  He-8/s

Capture efficiency  
 $1 \times 10^{-7}$

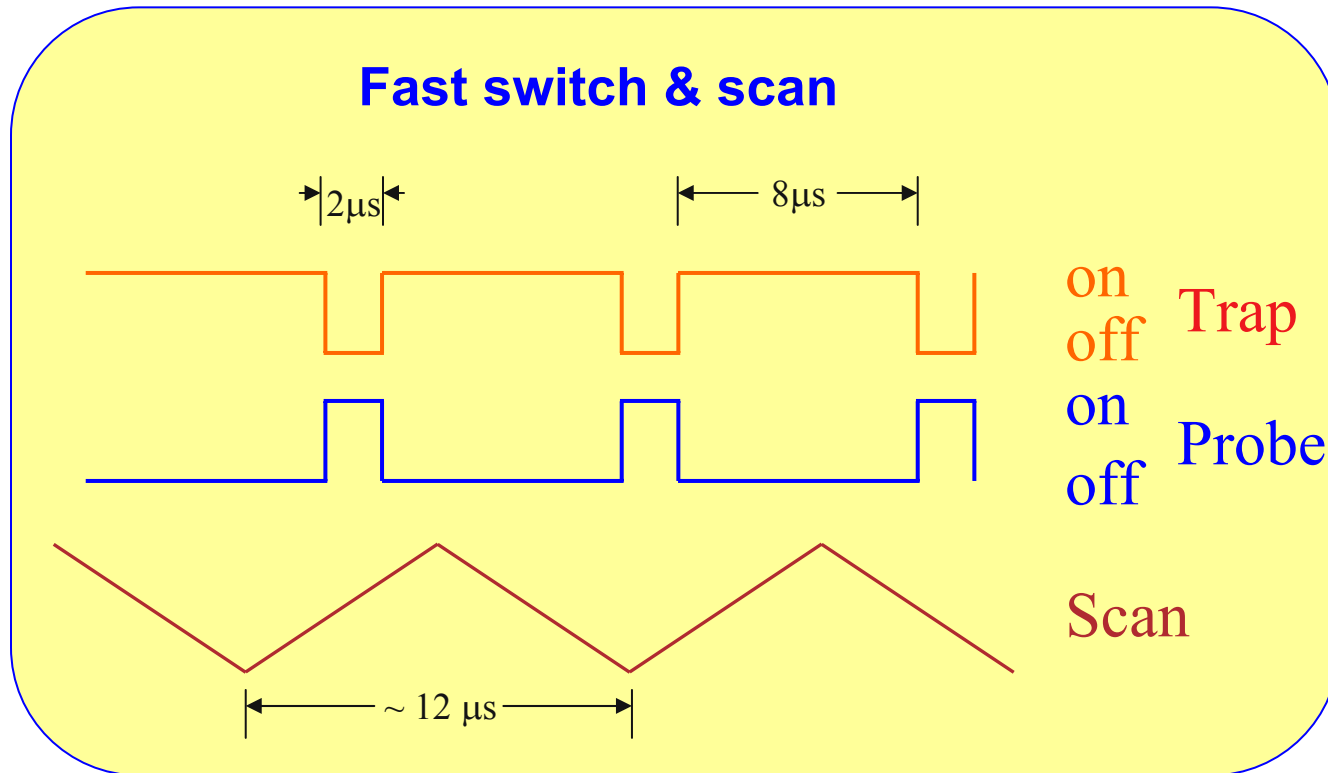
Trap  
 $\sim 5$  He-6/s,  
 $\sim 30$  He-8/hr



One trapped  ${}^6\text{He}$  atom



# Switch & Scan

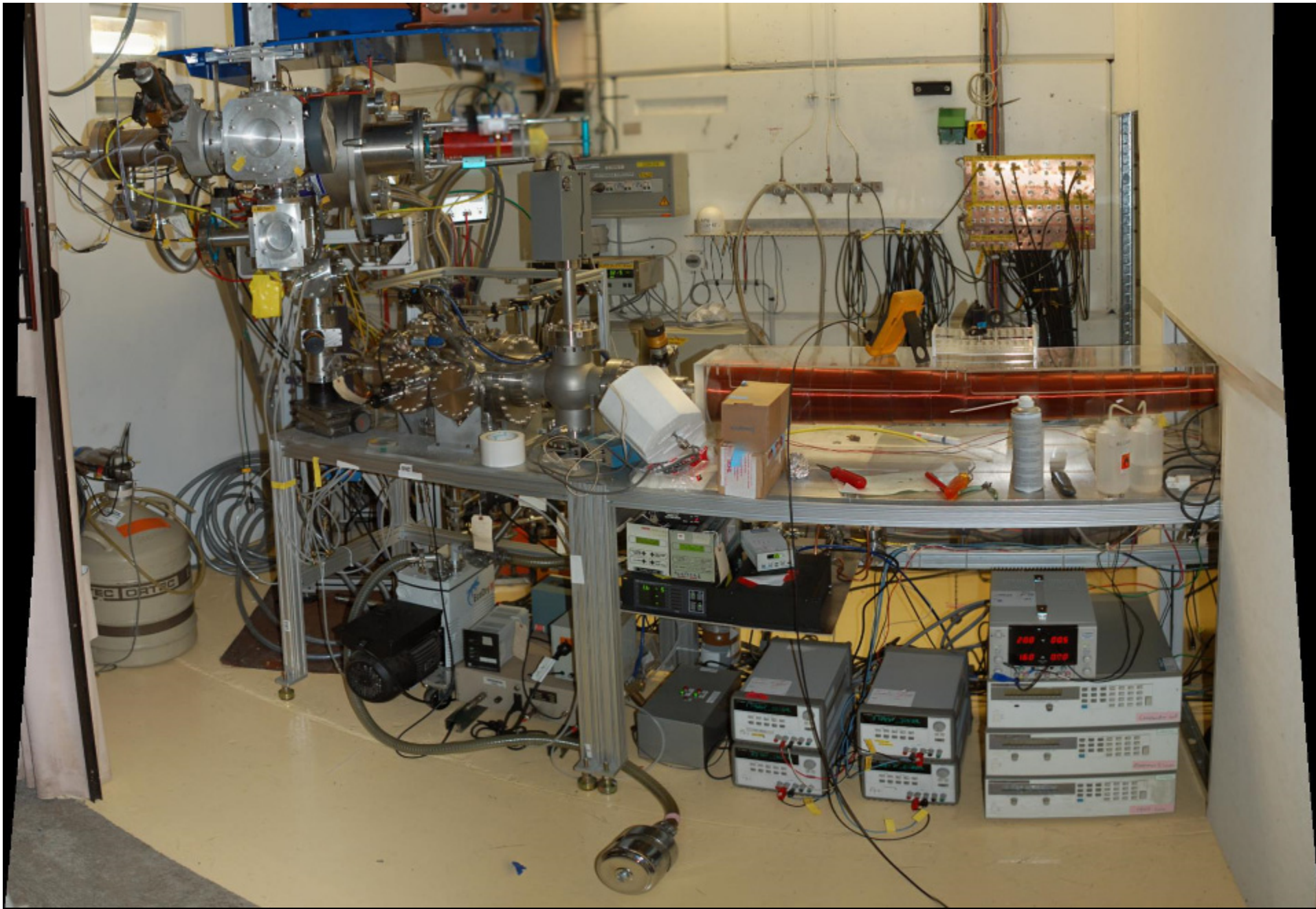




Jan. 26<sup>th</sup> 2007





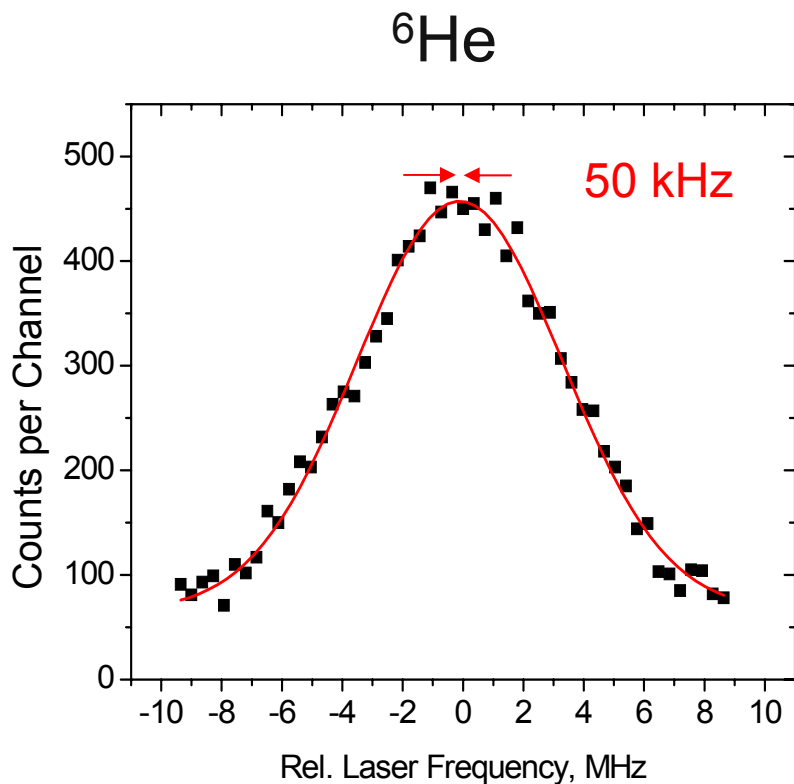




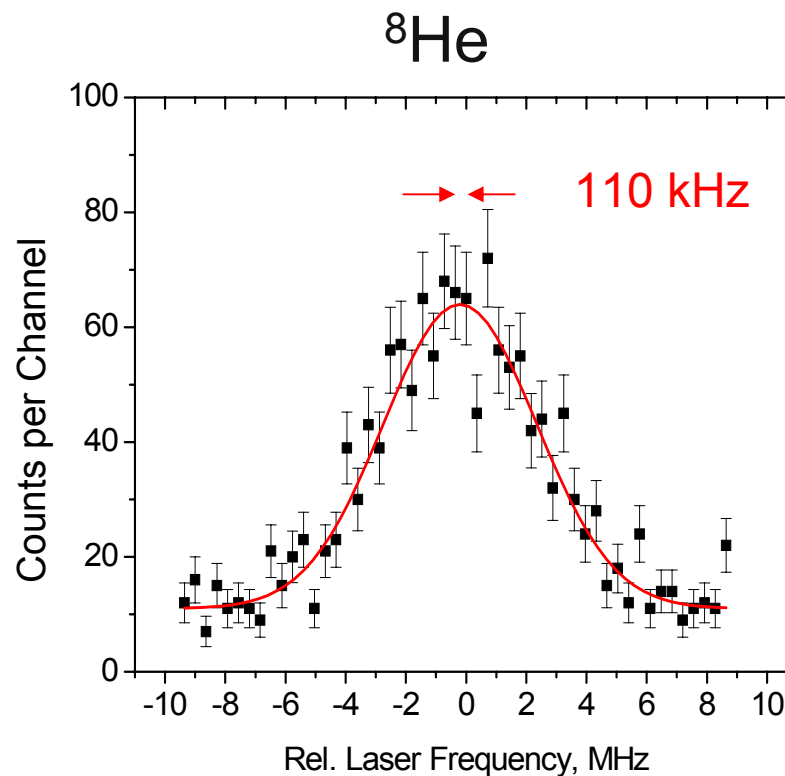




# ${}^6\text{He} + {}^8\text{He}$ Sample Spectra

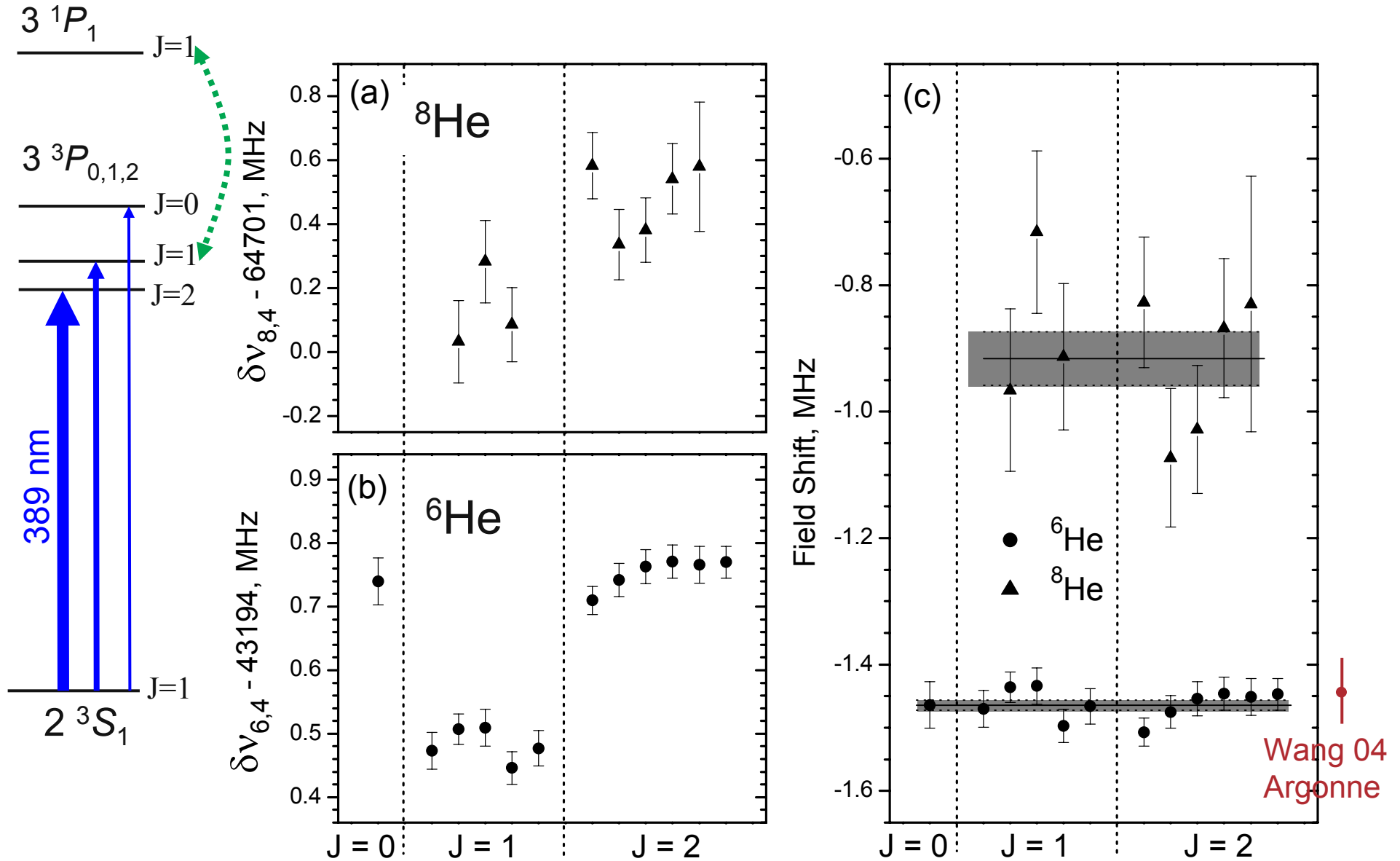


$\sim 5$   ${}^6\text{He}$  atoms/s  
2 minutes



$\sim 30$   ${}^8\text{He}$  atoms/hr  
2 hours

# Isotope Shift and Field Shift : J - Dependence?



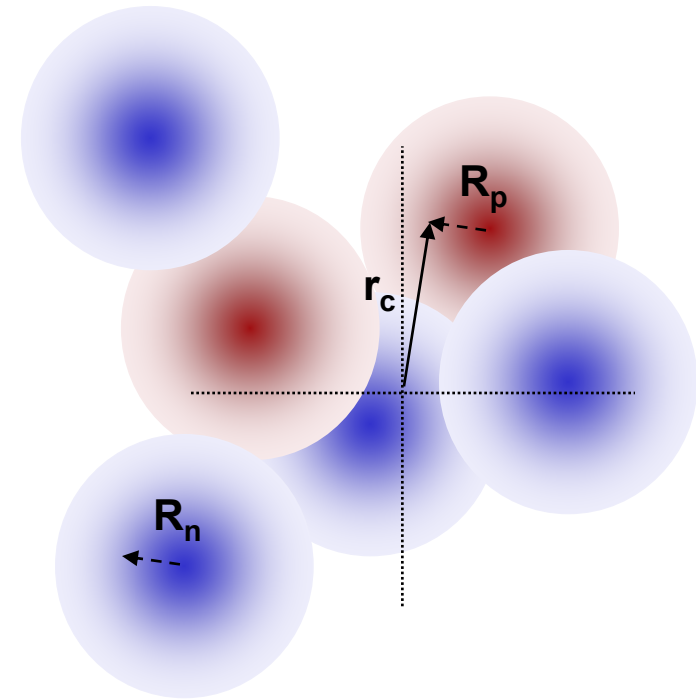
## Experimental Uncertainties and Corrections

		${}^6\text{He}$	${}^8\text{He}$
Statistical	Photon Counting	8 kHz	32 kHz
	Laser Alignment	2 kHz	12 kHz
	Reference Laser	2 kHz	24 kHz
Systematic	Probing Power Shift	0 kHz	15 kHz
	Zeeman Shift	<b>30 kHz</b>	45 kHz
	Nuclear Mass	15 kHz	<b>1 kHz</b>
	<b>TOTAL</b>	<b>35 kHz</b>	<b>63 kHz</b>
Corrections	Recoil Effect	+110(0) kHz	+165(0) kHz
	Nuclear Polarization	-14(3) kHz	-2(1) kHz

TITAN Penning Trap @ TRIUMF, V. L. Ryjkov *et al.*, PRL **101**, 012501 (2008)

## ${}^6\text{He}$ & ${}^8\text{He}$ RMS Charge Radii

	${}^6\text{He}$	${}^8\text{He}$
Field Shift, MHz	-1.464(34)	-1.026(63)
<b>RMS <math>R_{\text{CH}}</math>, fm</b>	<b>2.072(9)</b>	<b>1.961(16)</b>
Total Uncertainty	<b>0.4 %</b>	<b>0.9 %</b>
- Statistical	0.1 %	0.6 %
- Trap Systematics	0.3 %	0.6 %
- Mass Systematics	0.1 %	0.0 %
- He-4: 1.681(4) fm	0.1 %	0.1 %



$$\langle r^2 \rangle_{\text{pp}} = \langle r^2 \rangle_{\text{ch}} - \langle R_p^2 \rangle - \frac{3}{4M_p^2} - \frac{N}{Z} \langle R_n^2 \rangle$$

-  $\delta_{\text{SO}}$  - MEC

P. Mueller *et al.*, PRL **99**, 252501 (2007)

+ V. L. Ryjkov *et al.*, PRL **101**, 012501 (2008): He-8 mass

+ I. Sick PRC **77**, 041302(R) (2008): He-4 Charge Radius

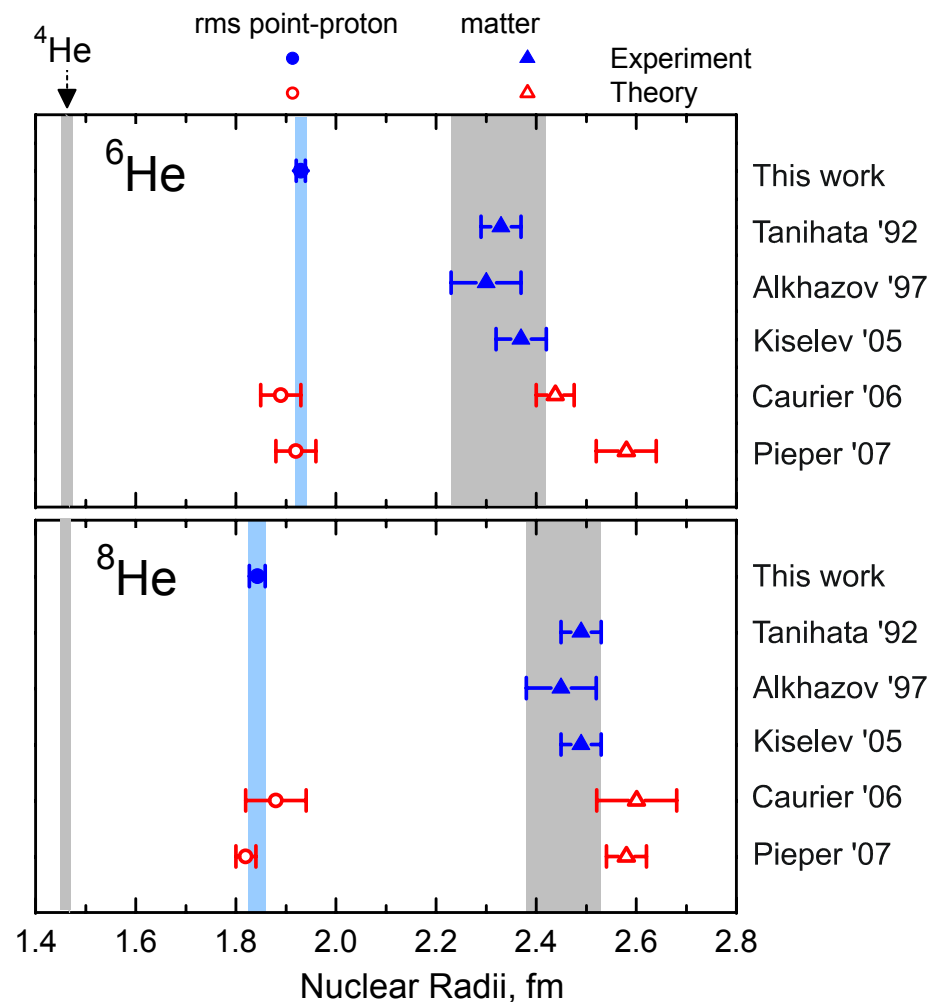
$$\langle R_p^2 \rangle = 0.766(12) \text{ fm}^2$$

$$\langle R_n^2 \rangle = -0.120(5) \text{ fm}^2$$

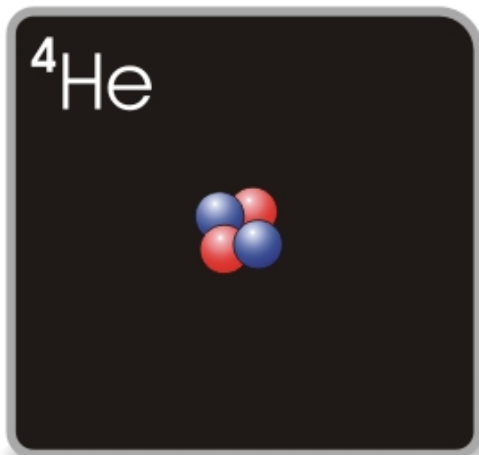
# ${}^6\text{He}$ & ${}^8\text{He}$ RMS Point Proton and Matter Radii

	${}^6\text{He}$	${}^8\text{He}$
Field Shift, MHz	-1.464(34)	-1.026(63)
<b>RMS <math>R_{pp}</math>, fm</b>	<b>1.930(9)</b>	<b>1.843(16)</b>
Total Uncertainty	<b>0.4 %</b>	<b>0.9 %</b>
- Statistical	0.1 %	0.6 %
- Trap Systematics	0.3 %	0.6 %
- Mass Systematics	0.2 %	0.0 %
- He-4: 1.465(4) fm	0.1 %	0.1 %

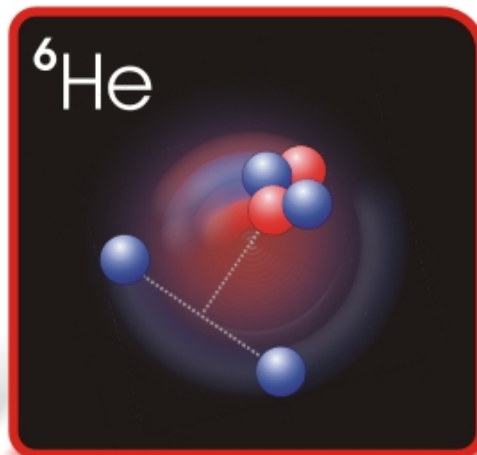
No Spin-Orbit and *MEC* ...



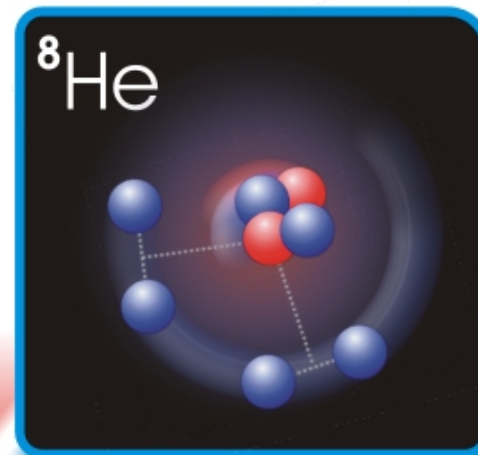
## RMS Charge Radii: ${}^4\text{He}$ - ${}^6\text{He}$ - ${}^8\text{He}$



1.681(4) fm



2.072(9) fm



1.961(16) fm

**Thank You!**



**<sup>6</sup>He Collaboration**

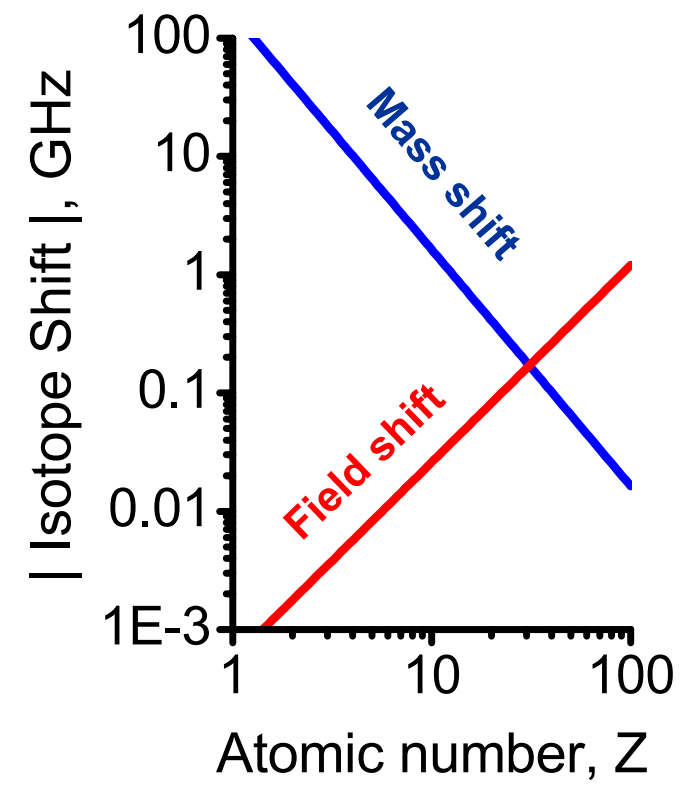
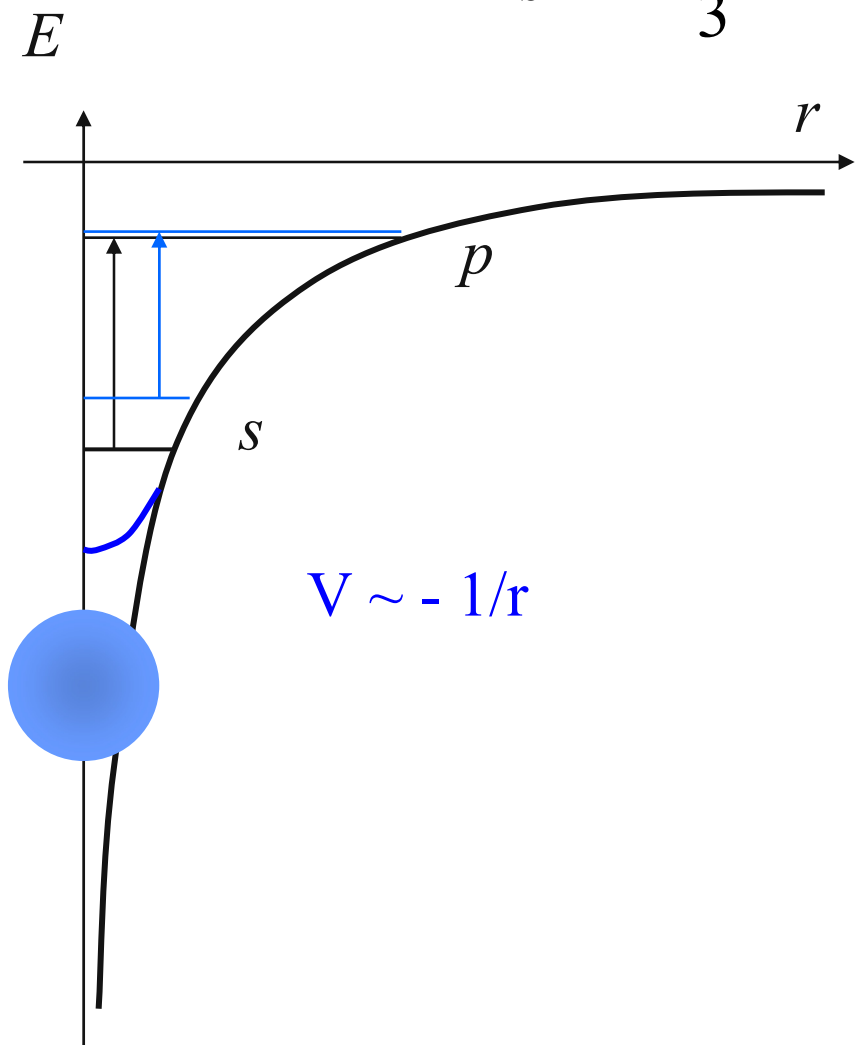
**P. Mueller, L.-B. Wang, K. Bailey, J.P. Greene, D. Henderson, R.J. Holt, R. Janssens, C.L. Jiang, Z.-T. Lu, T. O'Conner, R.C. Pardo, K.E. Rehm, J.P. Schiffer, X.D. Tang - *Physics Division, Argonne National Laboratory, USA***  
**G. W. F. Drake - *University of Windsor, Windsor, Canada***

**<sup>8</sup>He Collaboration**

**P. Mueller, K. Bailey, R. J. Holt, R. V. F. Janssens, Z.-T. Lu, T. P. O'Connor, I. Sulai - *Physics Division, Argonne National Laboratory, USA*; M.-G. Saint Laurent, J.-Ch. Thomas, A.C.C. Villari et al.- *GANIL, Caen, France***  
**G. W. F. Drake - *University of Windsor, Windsor, Canada*** **L.-B. Wang – *Los Alamos National Laboratory, USA***

# Field (Volume) Shift

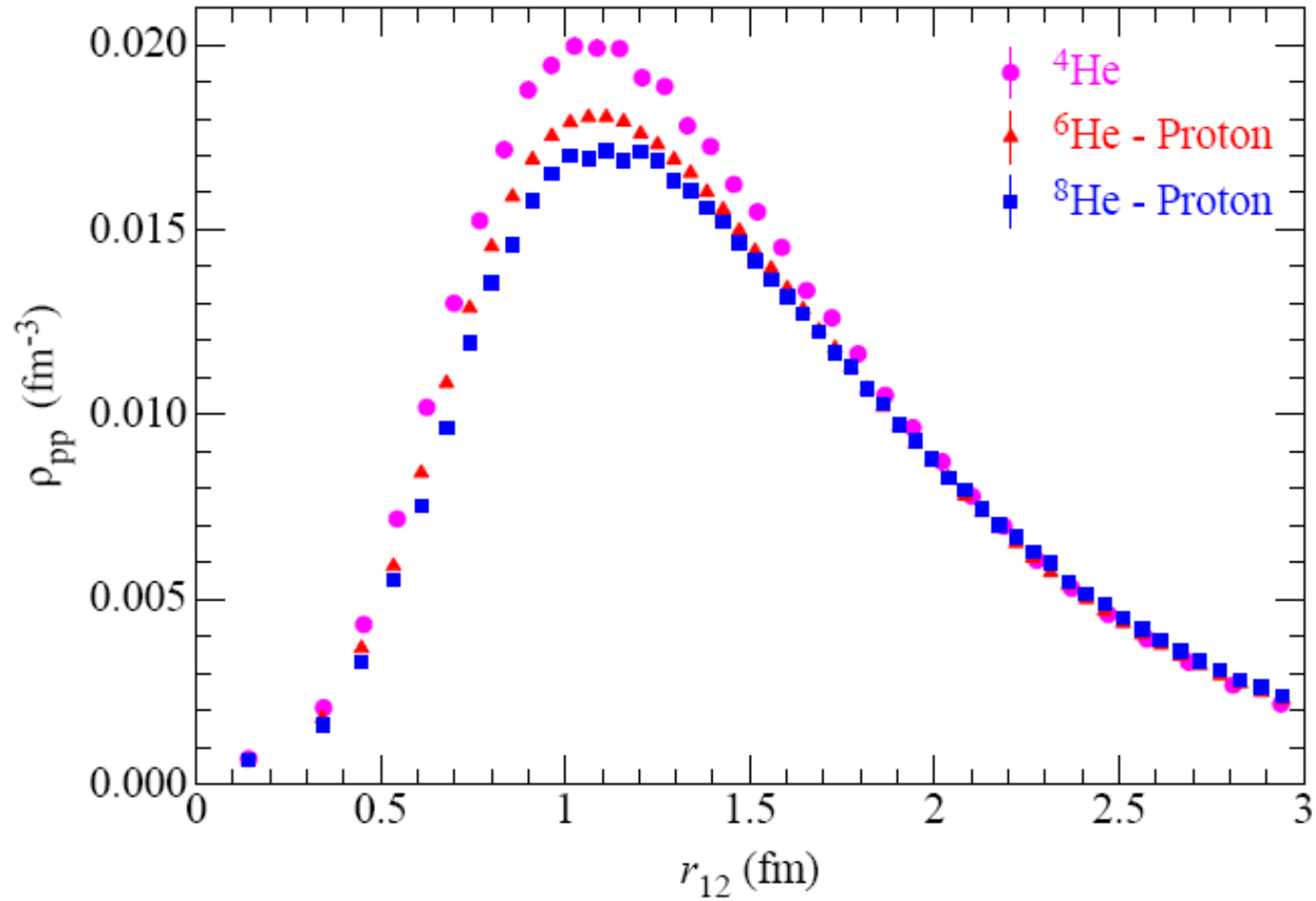
$$\delta v_{FS} = -\frac{2\pi}{3} Ze^2 \cdot \Delta|\Psi(0)|^2 \cdot \delta\langle r^2 \rangle^{AA'}$$



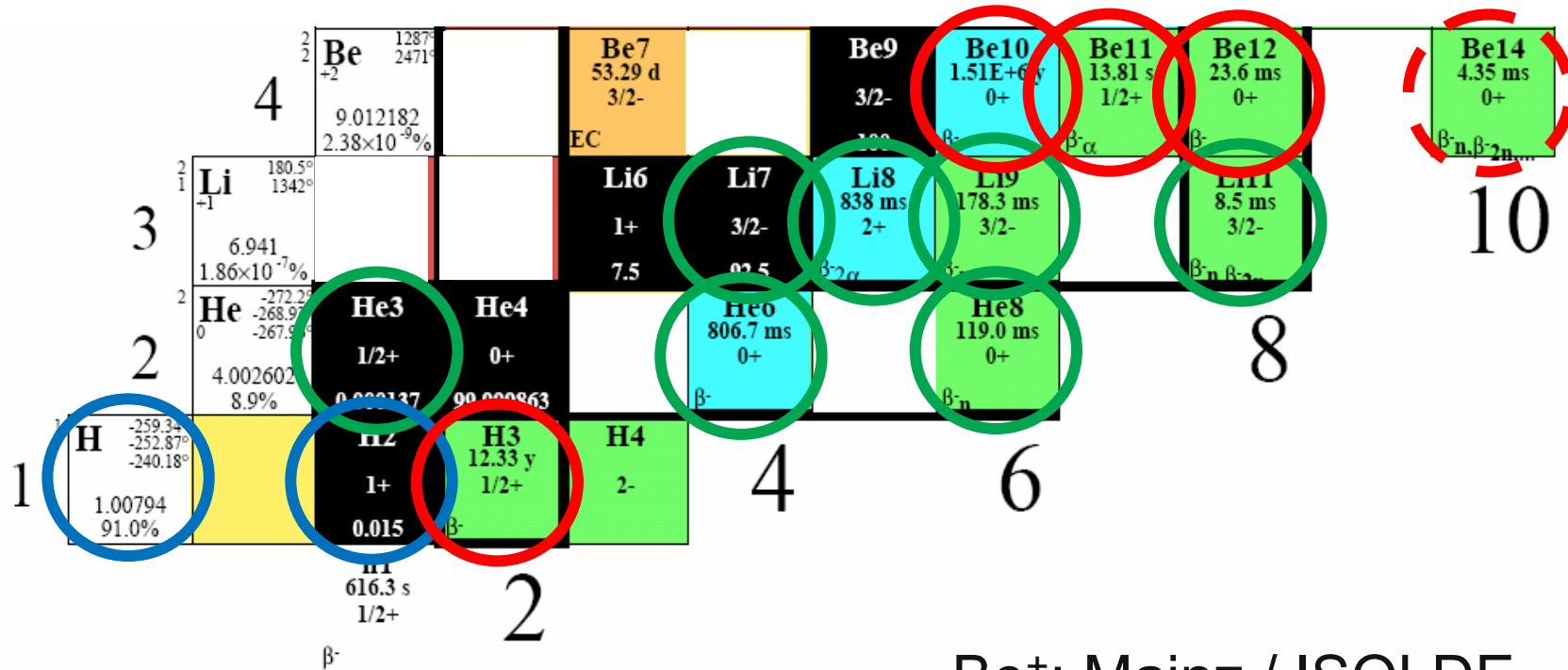


# GFMC – What happens to the $\alpha$ -core?

AV18 + IL2 GFMC proton-proton distributions



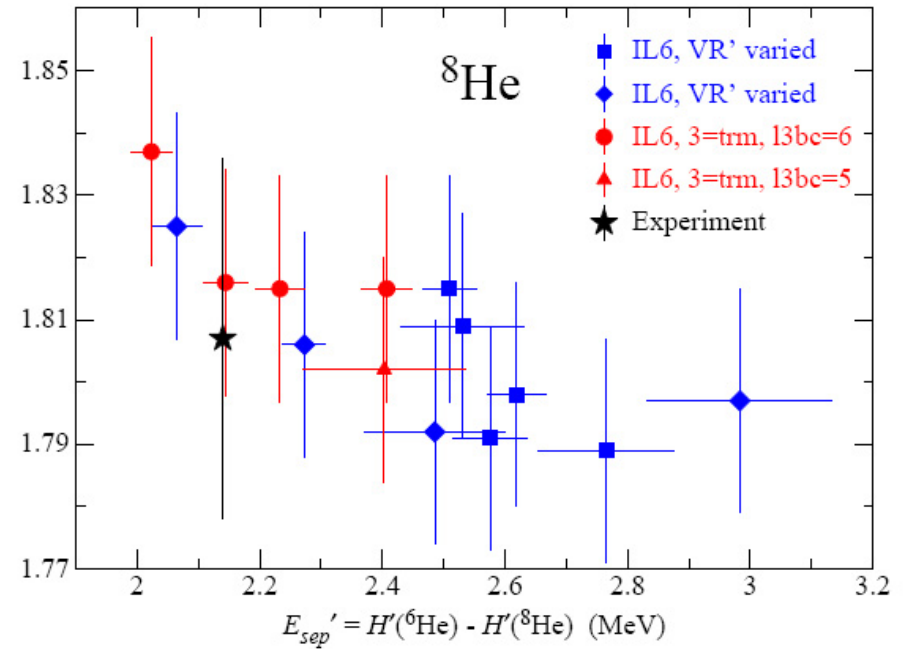
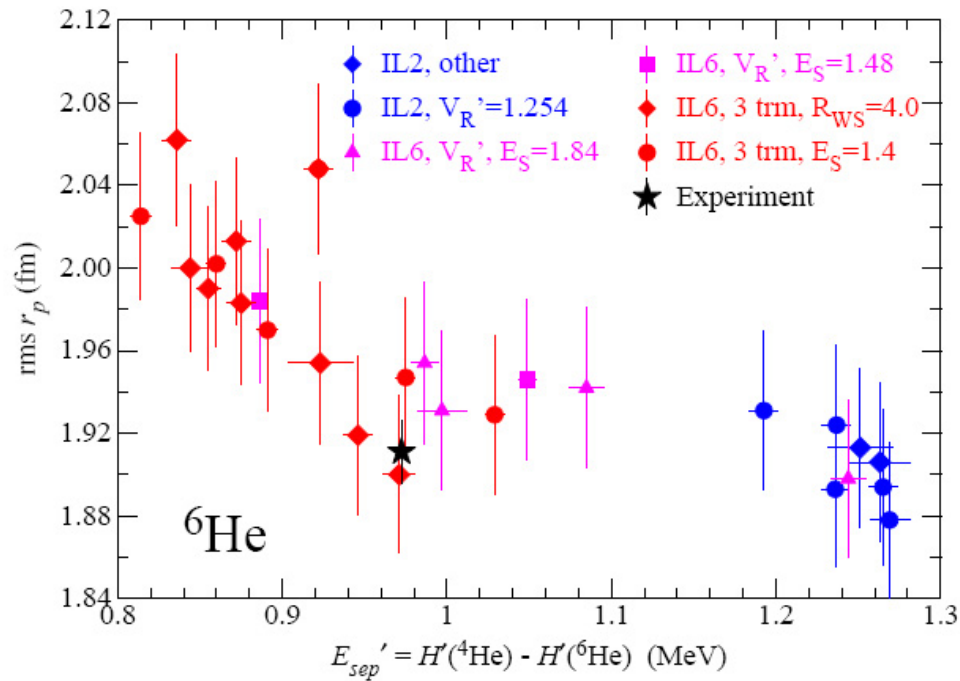
# Charge Radii of Light Isotopes by Laser Spectroscopy



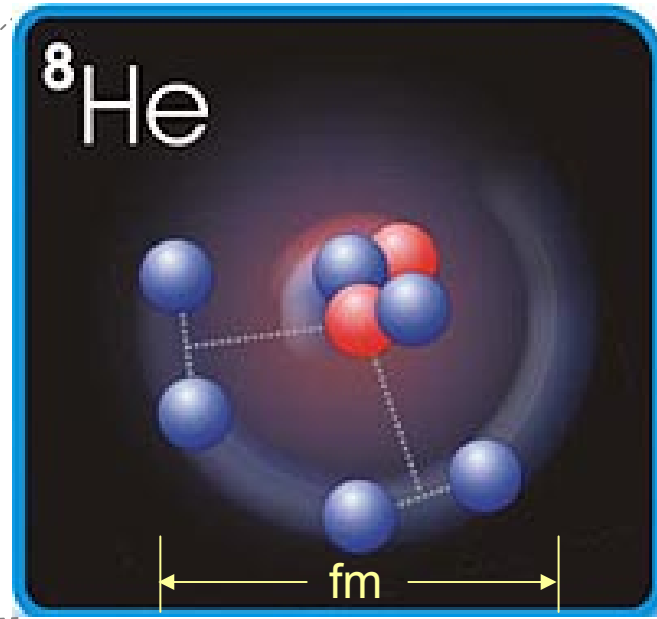
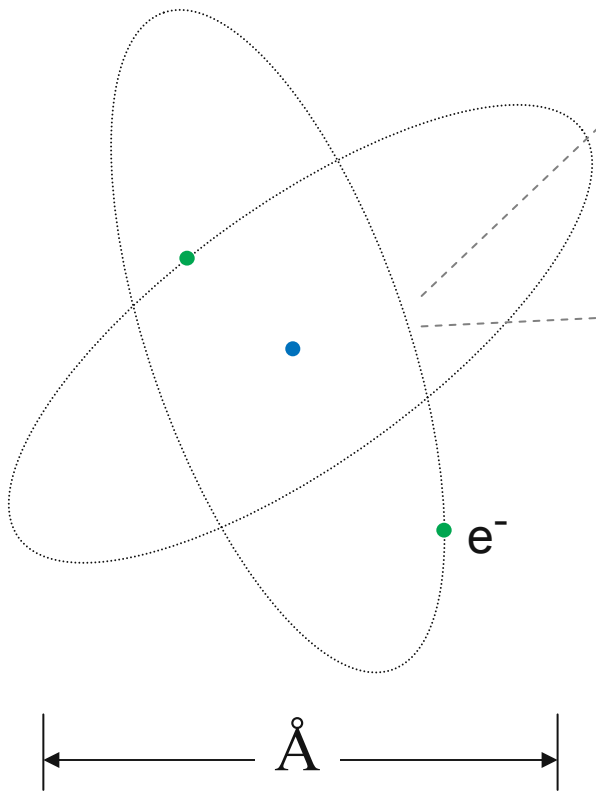
- Isotope Shift: ○
- IS+absolute  $\nu$ : ○
- In prep.: ○

- Be<sup>+</sup>: Mainz / ISOLDE
- Li: GSI / TRIUMF
- He: Argonne / GANIL
- H: MPQ Munich

# GFMC – Binding Energy vs. Charge Radius



# Helium Atom



## Ionization Energy of Helium Atom

Level  $2\ ^3S_1$

Calculation  $1\ 152\ 842\ 741 \pm 6\ \text{MHz}$

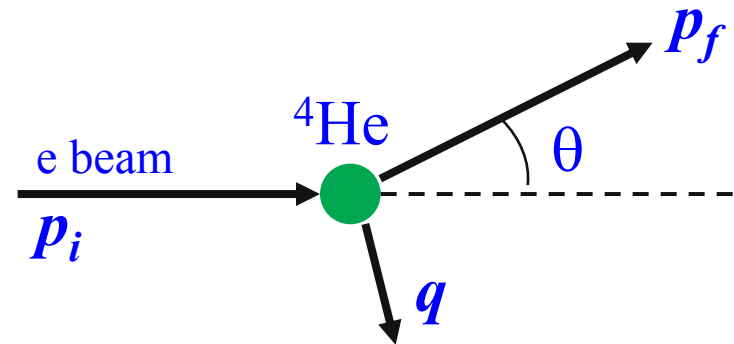
Experiment  $1\ 152\ 842\ 743\ \text{MHz}$

*Gordon Drake, Phys. Scripta (1999)*

## E&M Probe of Nuclear Charge Distribution

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{exp}} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \cdot |F(q^2)|^2$$

$$F(q^2) = 1 - \frac{1}{6} q^2 \langle r^2 \rangle_{\text{charge}} + \dots$$



mean-square radius  $\langle r^2 \rangle = \int \rho(r) \cdot r^2 dv$

root-mean-square radius  $\sqrt{\langle r^2 \rangle}$

${}^4\text{He}$  rms charge radius = 1.681(4) fm

[I. Sick *PRC* 77, 041302(R) (2008)]

## Conclusions & Outlook

- Precision laser spectroscopy and atomic physics  
test precision nuclear structure calculations of light, neutron rich isotopes  
at the ~1% level
- The charge radii will improve with ...
  - new He-6/8 mass measurement in Penning trap @ TRIUMF in Dec. '07
  - Improved value for He-4 (I. Sick, priv. comm.)
- Measurement at the 0.1% level (~ 10 kHz) for He are feasible ...  
if warranted

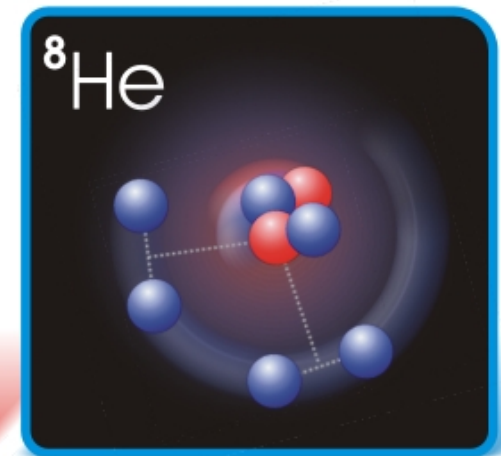
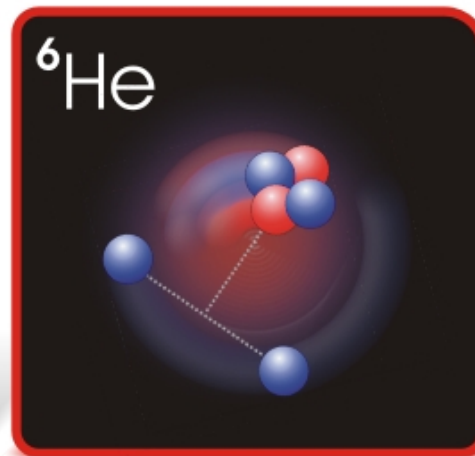
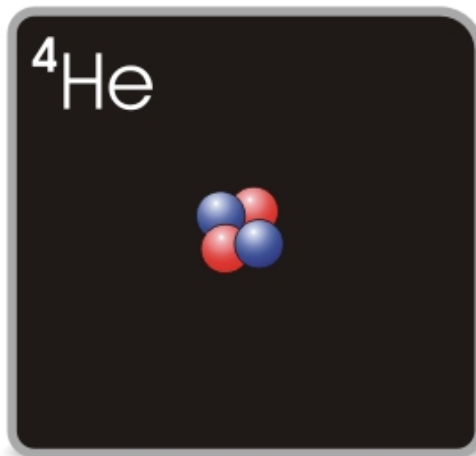
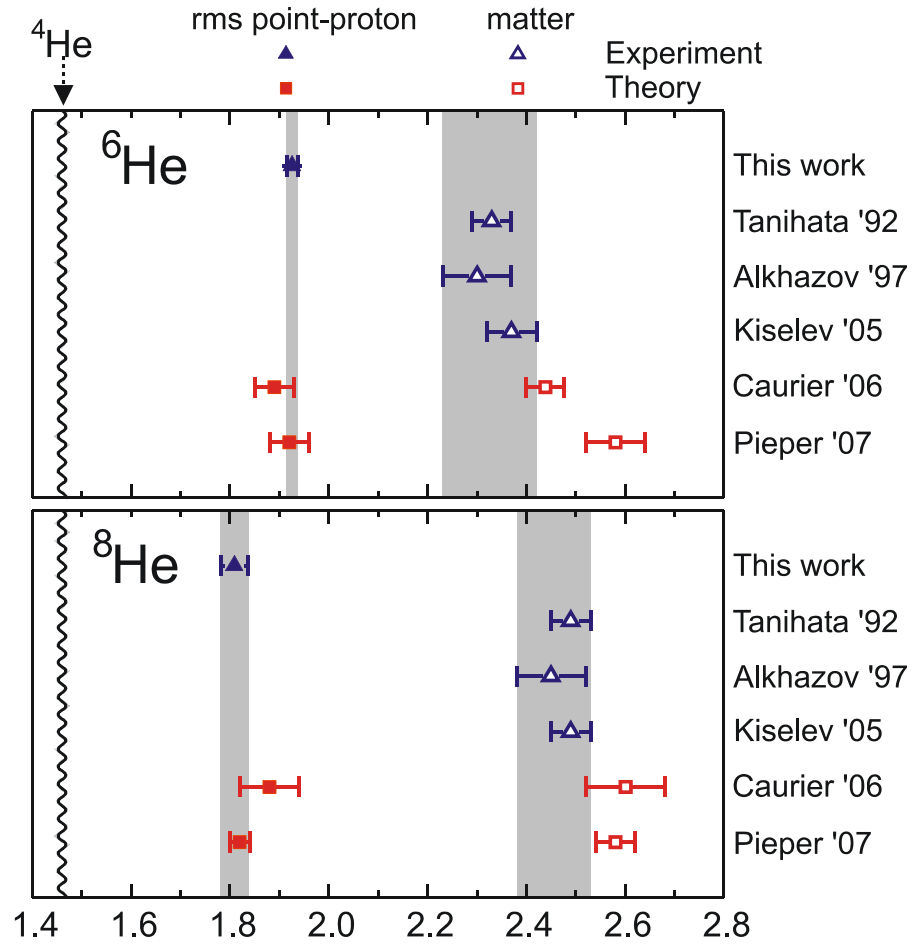
## ${}^6\text{He}$ & ${}^8\text{He}$ Charge Radii

	${}^6\text{He}$	${}^8\text{He}$
Field Shift, MHz	-1.464(34)	-0.916(95)
<b>RMS <math>R_{\text{CH}}</math>, fm</b>	<b>2.068(11)</b>	<b>1.929(26)</b>
Total Uncertainty	0.5 %	1.3 %
- Statistical	0.1 %	0.6 %
- Trap Systematics	0.3 %	0.6 %
- Mass Systematics	0.2 %	1.0 %
- He-4: 1.676(8) fm	0.3 %	0.4 %

P. Mueller *et al.*, PRL **99**, 252501 (2007)

L.-B. Wang *et al.*, PRL 93, 142501 (2004): 2.054(14) fm for He-6

# ${}^6\text{He}$ & ${}^8\text{He}$ Charge Radii



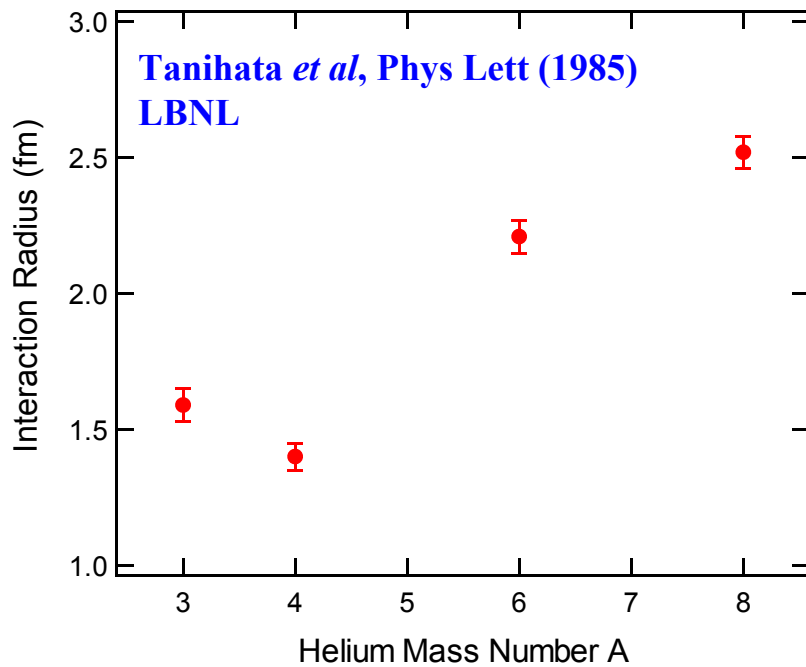
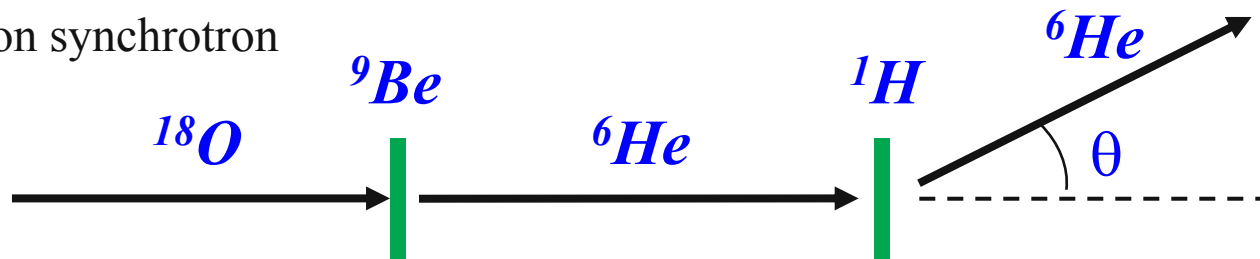


## Outline

- Neutron Halo Isotopes  ${}^{6,8}\text{He}$
- Charge Radii and Isotope Shift
- Atom Trapping of  ${}^{6,8}\text{He}$  @ Argonne and GANIL
- ${}^8\text{He}$  Larger or Smaller than  ${}^6\text{He}$ ?

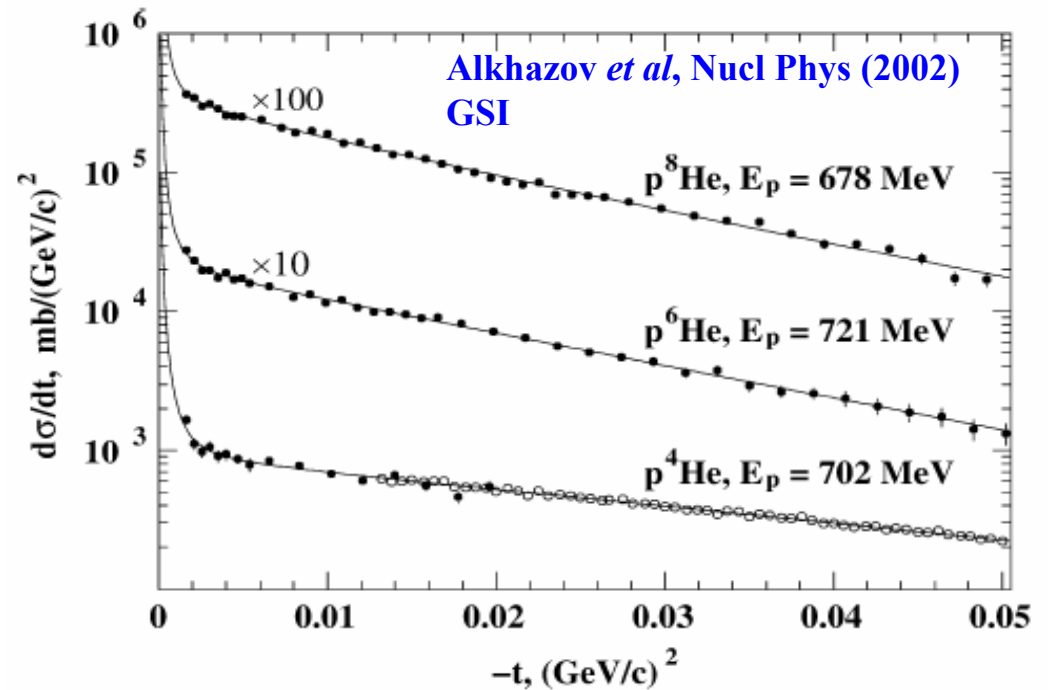
# Hadronic Probe: Scattering of ${}^6\text{He}$ & ${}^8\text{He}$ Beams

GSI heavy-ion synchrotron



Elastic and inelastic collision: He on C, B

$$\sigma_I(6\text{He}) - \sigma_I(4\text{He}) = \sigma_{-2n}(6\text{He})$$



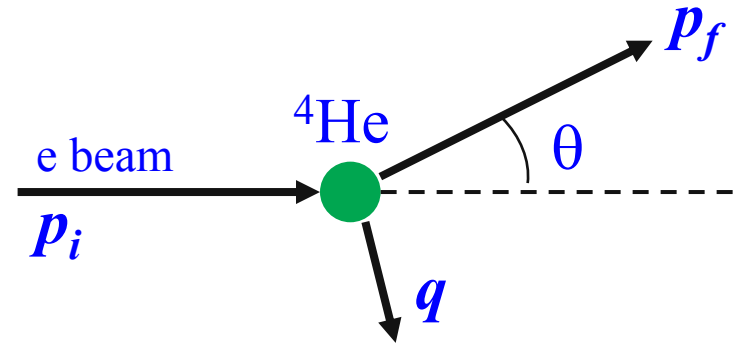
Elastic collision: He on proton, 700 MeV/u

Matter distribution, matter radii

## E&M Probe of Nuclear Charge Distribution

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{exp}} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \cdot |F(q^2)|^2$$

$$F(q^2) = 1 - \frac{1}{6} q^2 \langle r^2 \rangle_{\text{charge}} + \dots$$



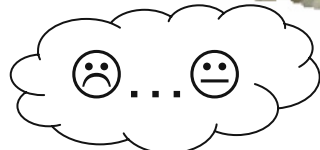
mean-square radius  $\langle r^2 \rangle = \int \rho(r) \cdot r^2 dv$

root-mean-square radius  $\sqrt{\langle r^2 \rangle}$

${}^4\text{He}$  rms charge radius = 1.676(8) fm [I. Sick Phys Lett B (1982)]

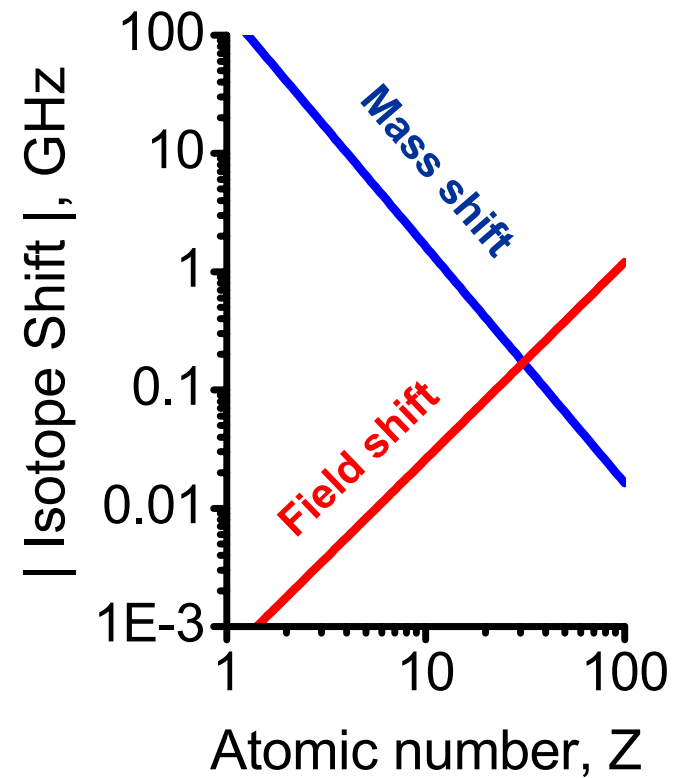
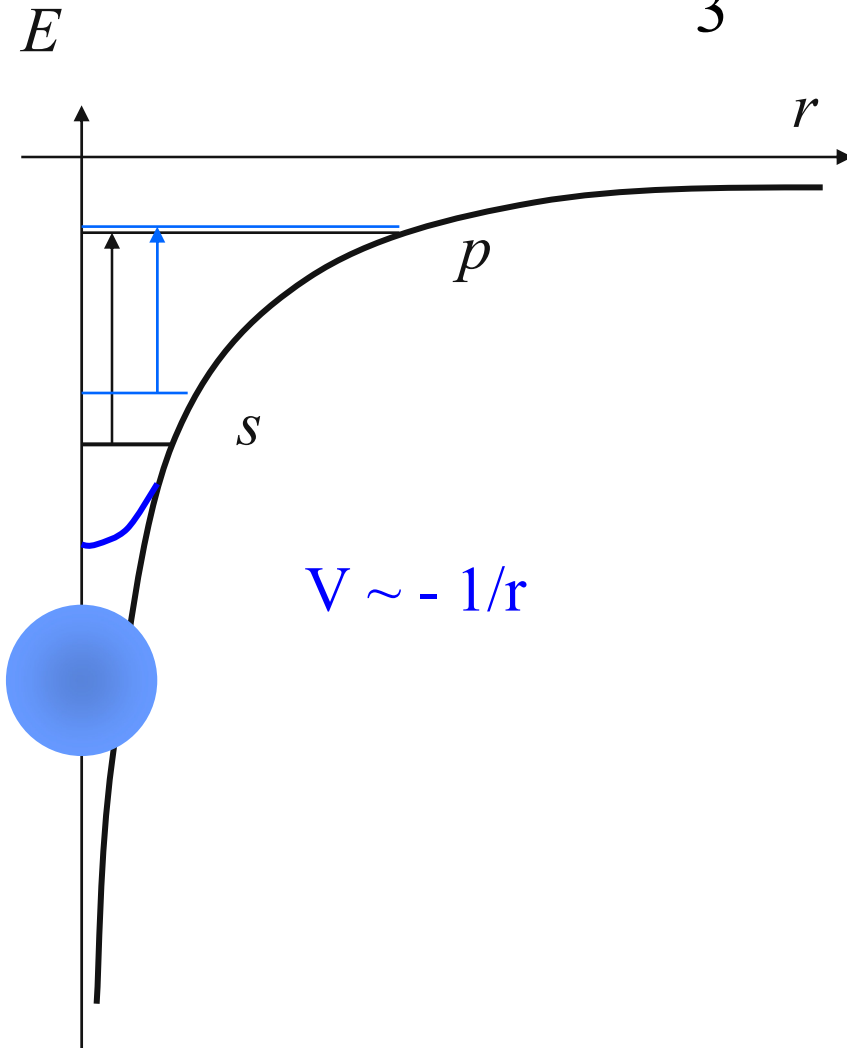
Proton rms charge radius = 0.895(18) fm [I. Sick Phys Lett B (2003)]

# June 14<sup>th</sup> .... Trip to Brittany



# Field (Volume) Shift

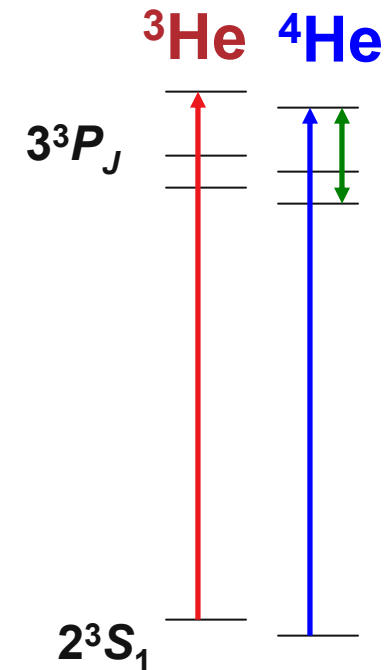
$$\delta v_{FS} = -\frac{2\pi}{3} Ze^2 \cdot \Delta|\Psi(0)|^2 \cdot \delta\langle r^2 \rangle^{AA'}$$



# Atomic Theory of Helium

Gordon W.F. Drake (*Can. J. Phys* **84**, 83 2006)

- ◆ Non-relativistic wave functions from variational calculations
- ◆ Perturbation theory for relativistic corrections, QED, *finite nuclear mass* and *nuclear charge radius*
- ◆ QED terms “cancel” in isotope shift



## Experimental confirmation

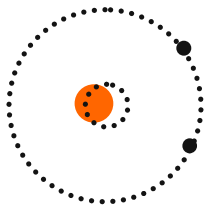
- ◆ Total transition frequency F.S. Pavone *et al.*, PRL **73**, 42 (1994)
- ◆  $^4\text{He}$  Fine structure splitting P. Mueller *et al.*, PRL **94**, 133001 (2005)
- ◆  $^3\text{He}$ - $^4\text{He}$  Isotope shift + HFS I. Sulai *et al.*, *in preparation*

# Atomic Isotope Shift

$$\text{Isotope Shift} \quad \delta\nu = \delta\nu_{\text{MS}} + \delta\nu_{\text{FS}}$$

Mass shift:

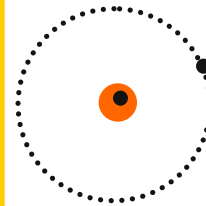
due to nuclear recoil



$$\delta\nu_{\text{MS}} \propto \frac{A - A'}{AA'}$$

Field shift:

due to charge distribution



$$\delta\nu_{\text{FS}} \propto Z \times \Delta[\Psi(0)]^2 \times \delta\langle r^2 \rangle$$